

Modeling Population Dynamics Using Count Data

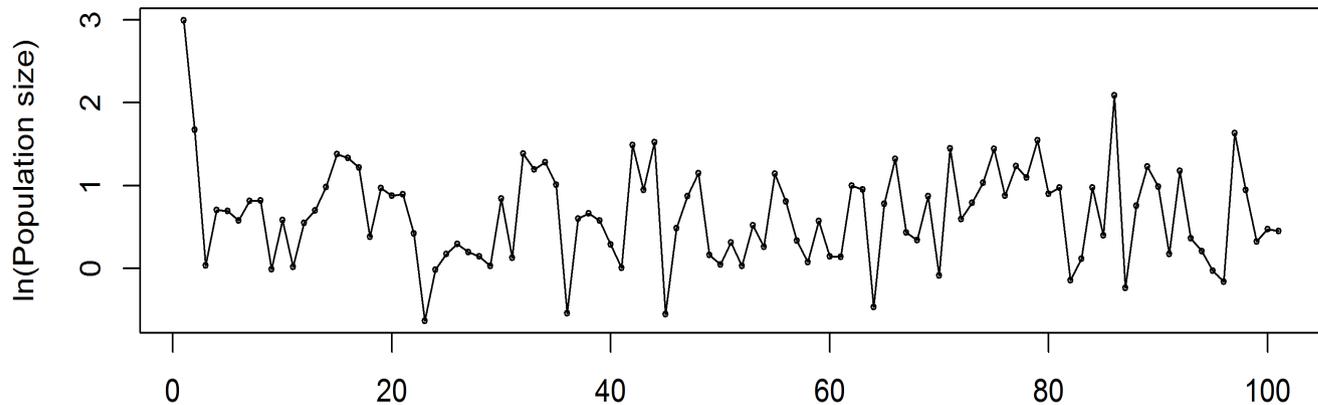
Outline

- A. Objectives, background
- B. Traditional models of population dynamics
 - Exponential, logistic, Ricker, Gompertz, etc...
 - State-space models, *a la* De Valpine and Hastings (2002)
 - **R** exercise
- C. Open population N -mixture models
 - Kery et al. (2009) model
 - Dail and Madsen (2011) model
 - **R** exercise

Objectives

Traditional models

- Estimate population growth rate
- Demographic contributions to growth
- Population viability analysis
- Test for density dependence



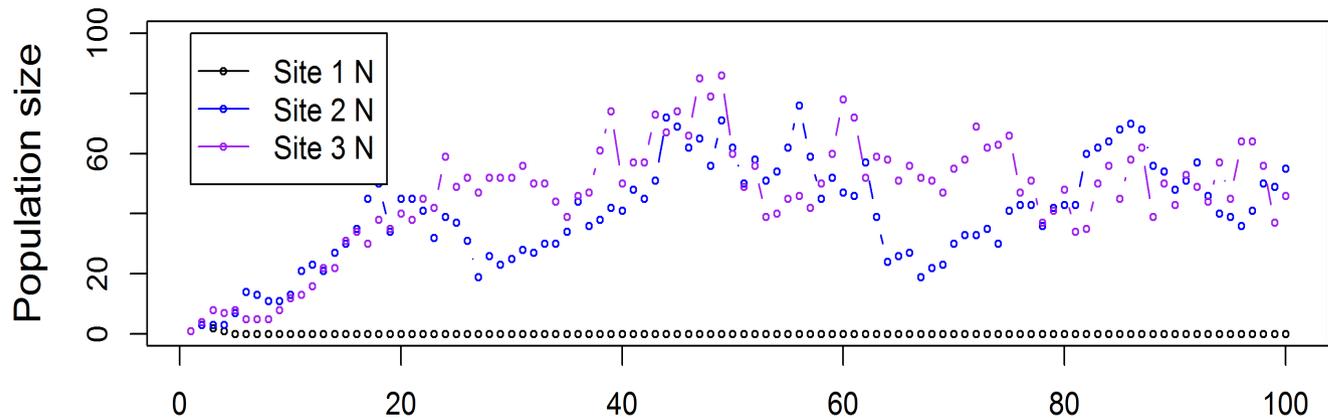
Objectives

Traditional models

- Estimate population growth rate
- Demographic contributions to growth
- Population viability analysis
- Test for density dependence

N -mixture models

- Estimate population size
- Model spatial variation in abundance
- Account for imperfect detection



Demographic Contributions to Population Growth

Open population: A population whose abundance (N) changes during some time interval due to births (B), deaths (D), immigration (I) or emigration (E).

$$N_t = N_{t-1} + B + I - D - E$$

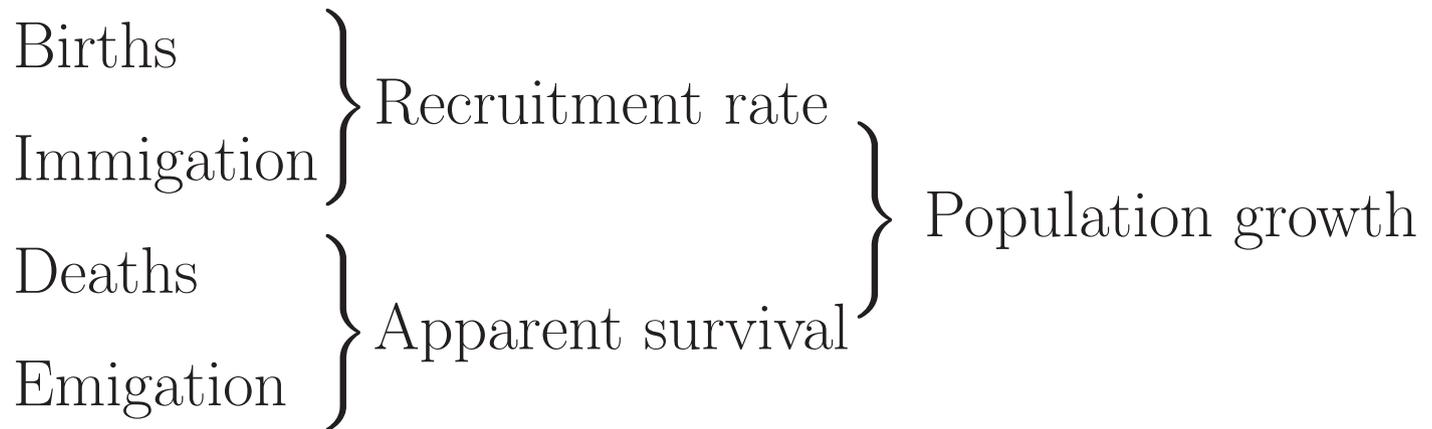
Demographic Contributions to Population Growth

Impossible to estimate each of these parameters without marked individuals.
But we (possibly) can estimate reduced information parameters.

Births	}	Recruitment rate
Immigration		
Deaths	}	Apparent survival
Emigration		

Demographic Contributions to Population Growth

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Modeling Approaches

Non-spatial, vital rates not estimated

- Count data (May, 1976; De Valpine and Hastings, 2002; Dennis et al., 2006)

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Spatial, vital rates not estimated

- Count data (Kery et al., 2009)

Spatial, vital rates possibly estimated

- Capture-recapture data (Nichols et al., 2000; Gardner et al., 2010)
- Count data (Dail and Madsen, 2011)

Classical Models of Population Growth

Exponential

$$N_{t+1} = N_t e^r = N_t \lambda$$

Logistic

$$N_{t+1} = N_t r (1 - N_t / K)$$

Ricker

$$N_{t+1} = N_t e^{r(1 - N_t / K)}$$

Gompertz

$$X_{t+1} = a + cX_t$$

State-space Models

Estimate process noise and observation error.

$$X_{t+1} = a + cX_t + \epsilon_t$$

$$\epsilon_t \sim \text{Normal}(0, \sigma^2)$$

$$Y_t \sim \text{Normal}(X_t, \tau^2)$$

X_t = log-transformed abundance at time t

σ^2 = variance of random process variation

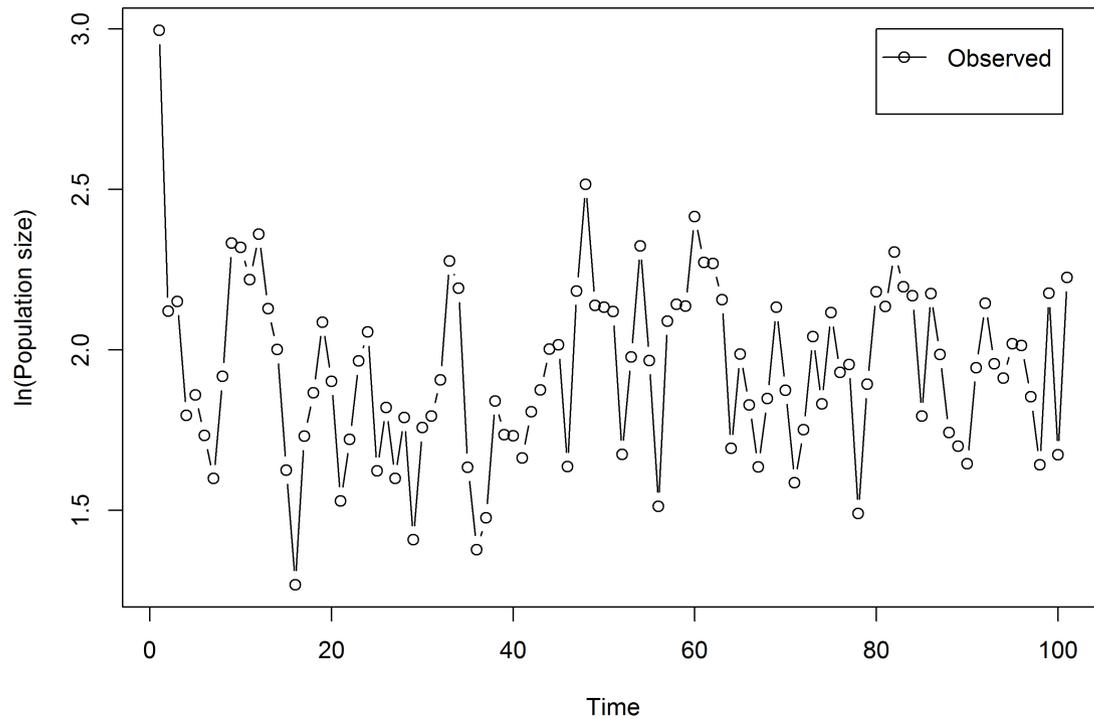
Y_t = log-transformed count at time t

τ^2 = variance of random observation error

a = intrinsic rate of increase

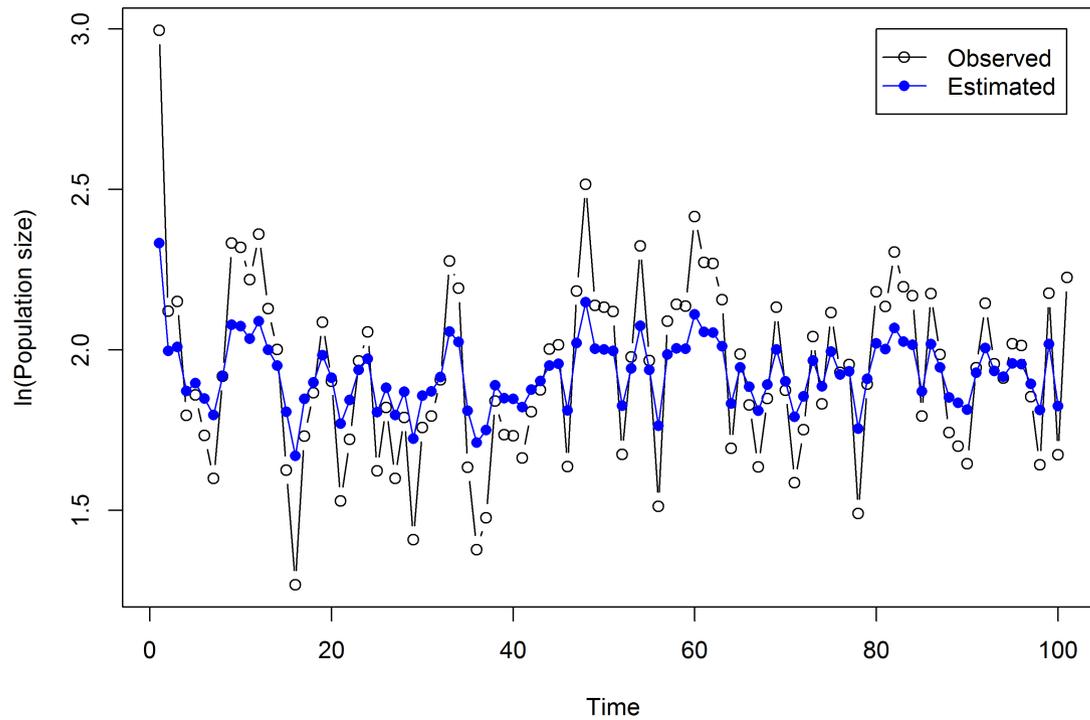
c = strength of density dependence

State-space Models



State-space Models

$\hat{a}=1.18$ $\hat{c}=0.38$ $\hat{\sigma}=0.23$ $\hat{\tau}=0.15$



State-space Models

R exercise:

Fitting State-space Models

OPEN `script-state-space.R`

State-space Models

Limitations of standard state-space models

- Ignore spatial variation
- Implausible model for observation error
- Demographic contributions to pop growth ignored
- Parameters are weakly identified

Open Population N -mixture Models

Key advantages

- Spatial and temporal variation can be modeled
- Observation error has clear interpretation
- Actual population size can be estimated in some cases

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Three varieties

- Temporary emigration (Chandler et al., 2011)
- Trend (Kery et al., 2009)
- Demographic (Dail and Madsen, 2011)

Open Population N -mixture Models

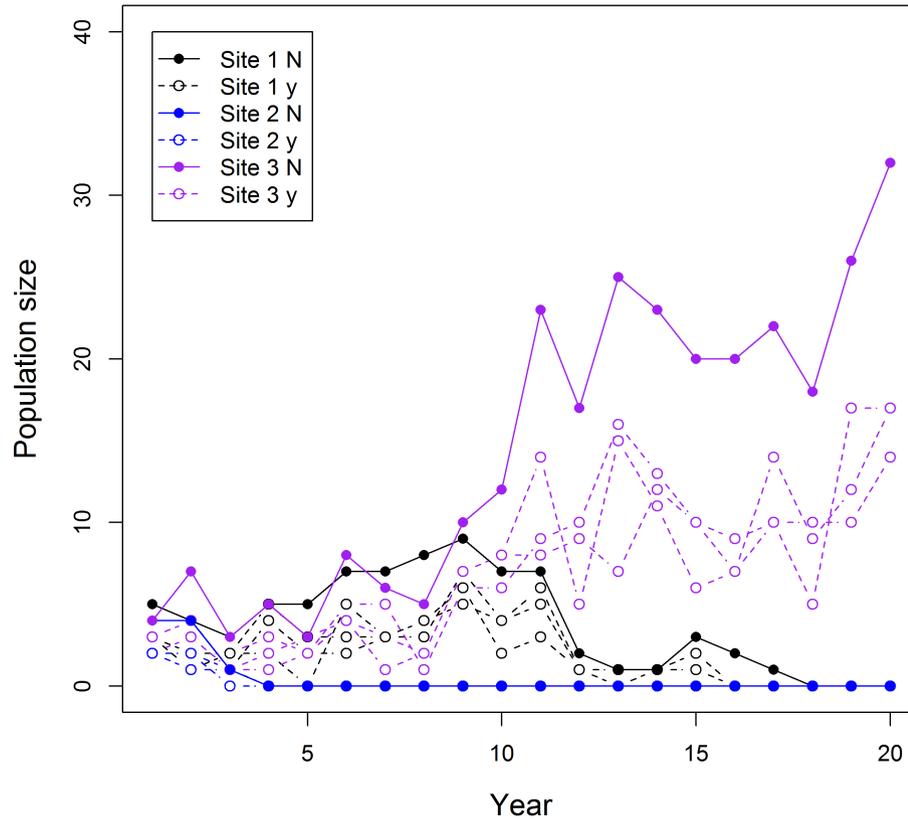
- Data

y_{ijt} = count at site i during secondary period j within primary period t .

Table 1: Count data with $R = 4$ sites, $T = 2$ primary periods and $J = 3$ secondary periods.

	Season 1			Season 2		
	visit 1	visit 2	visit 3	visit 1	visit 2	visit 3
site1	3	3	2	0	0	0
site2	0	0	0	2	4	3
site3	2	0	0	0	0	2
site4	0	0	2	0	0	1

Open Population N -mixture Models



Open Population N -mixture Models

Closed population model (Royle, 2004)

$$N_i \sim \text{Poisson}(\lambda_i)$$
$$y_{ij} \sim \text{Binomial}(N_i, p)$$

N_i — latent variable, population size at site i

λ_i — expected population size at site i

p — detection probability

Open Population N -mixture Models

Temporary emigration model (Chandler et al., 2011)

$$M_i \sim \text{Poisson}(\lambda)$$

$$N_{it} \sim \text{Binomial}(M_i, \phi)$$

$$y_{ijt} \sim \text{Binomial}(N_{it}, p)$$

M_i — latent variable, super population size at site i

N_{it} — latent variable, abundance at site i during time t

λ — expected superpopulation size

ϕ — probability of being exposed to sampling (1-temporary emigration)

p — detection probability

Open Population N -mixture Models

Trend model (Kery et al., 2009)

$$\begin{aligned}N_{it} &\sim \text{Poisson}(\lambda_{it}) \\ \log(\lambda_{it}) &= \alpha + r \times \text{year}_t \\ y_{ijt} &\sim \text{Binomial}(N_{it}, p)\end{aligned}$$

where

N_{it} = abundance at site i during year t

λ_{it} = expected abundance at site i during year t

r_i = is a “trend” parameter

y_{ijt} = observed count at site i , replicate j , and year t

p = detection probability

Open Population N -mixture Models

R exercise:

Fit Kery et al. (2009) N -mixture model to lizard data
using **JAGS**

OPEN script-lizard.R

Open Population N -mixture Models

Demographic model (Dail and Madsen, 2011)

$$\begin{aligned}N_{i1} &\sim \text{Poisson}(\lambda) \\S_{it} &\sim \text{Binomial}(N_{it-1}, \omega) \\G_{it} &\sim \text{Poisson}(N_{it-1}\gamma) \\N_{it} &= S_{it} + G_{it} \\y_{ijt} &\sim \text{Binomial}(N_{it}, p)\end{aligned}$$

N_{it} — latent variable, abundance at site i during year t

S_{it} — latent variable, survivors

G_{it} — latent variable, recruits

λ — mean abundance during $t = 1$

ω — apparent survival

γ — recruitment rate

p — detection probability

Open Population N -mixture Models

Simpler alternative, exponential growth model

$$\begin{aligned}N_{i1} &\sim \text{Poisson}(\lambda) \\N_{it} &\sim \text{Poisson}(\gamma N_{it-1}) \\y_{ijt} &\sim \text{Binomial}(N_{it}, p)\end{aligned}$$

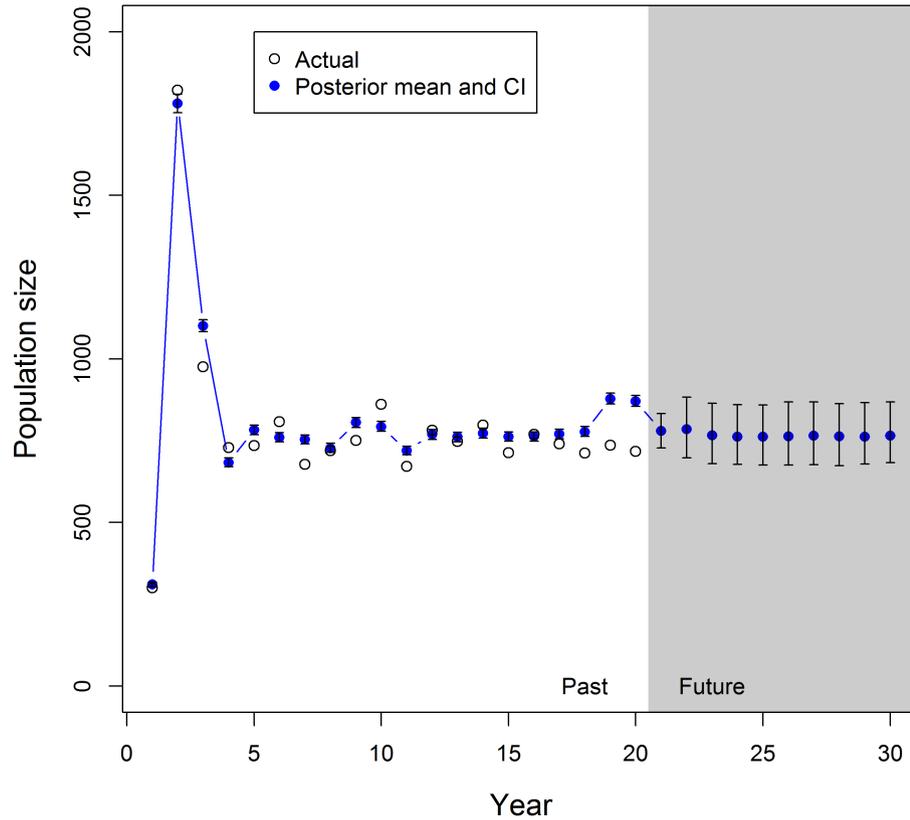
N_{it} — latent variable, abundance at site i during year t

λ — mean abundance during $t = 1$

γ — finite rate of increase

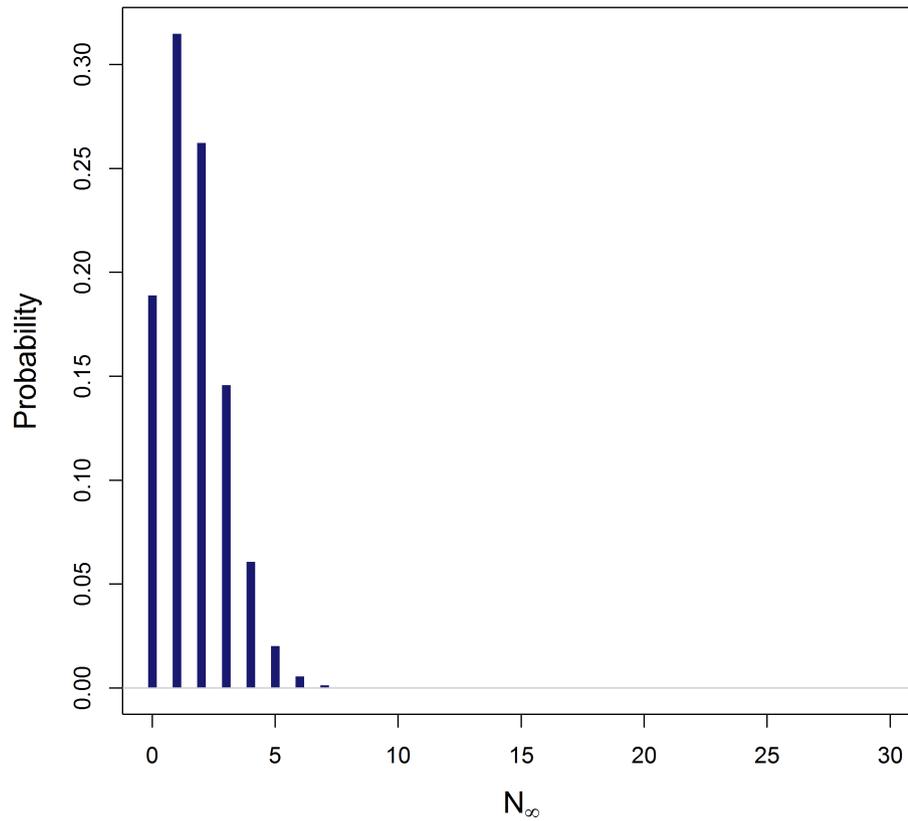
p — detection probability

Population projections



Population projections

Probability distribution at equilibrium



Exercise



photo credit: Mikey Lutmerding

Open Population N -mixture Models

R exercise:

Fit open N -mixture models to simulated data and
BBS data using `pcountOpen` and `JAGS`

`OPEN` script-dailMad.R

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