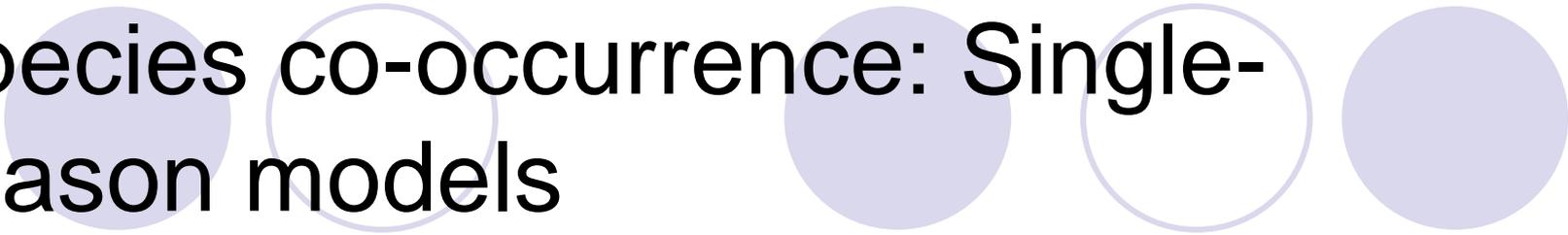


Species Co-occurrence

Species co-occurrence: Single-season models



- Do some species tend to occur more (or less) often together than expected?
- A great deal of literature has been published during past 30 years on methods for assessing *patterns* of co-occurrence, but not accounting for detectability.

Species co-occurrence matrix

		Species				
		1	2	3	4	5
Units	1	1	0	0	1	0
	2	1	1	0	0	1
	3	0	1	1	1	0
	4	1	0	0	0	1
	5	1	1	0	1	0

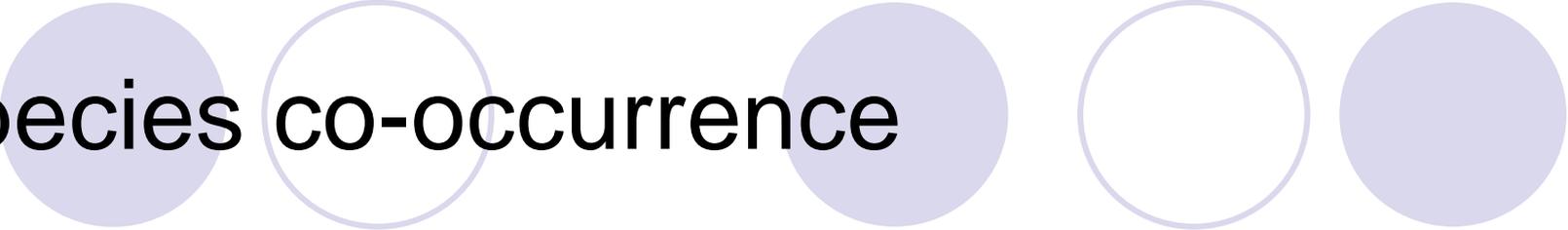
	<i>s</i>	1	0	0	1	1

Species co-occurrence matrix

		Species				
		1	2	3	4	5
Units	1	11	01	01	10	00
	2	10	11	00	01	11
	3	00	10	11	11	01
	4	10	00	00	00	10
	5	11	10	01	11	00

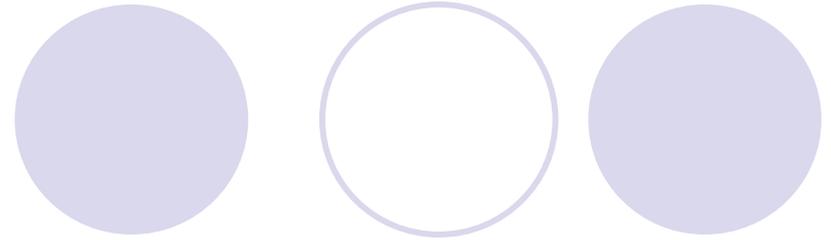
	s	11	01	00	10	11

Species co-occurrence



- Direction of interaction may be correctly estimated, but the magnitude of the interaction underestimated, if probability of detecting a species is the same regardless of whether the other species is also present.
- If detectability of a species differs given the presence/absence of the other species, estimated interaction may be completely misleading.

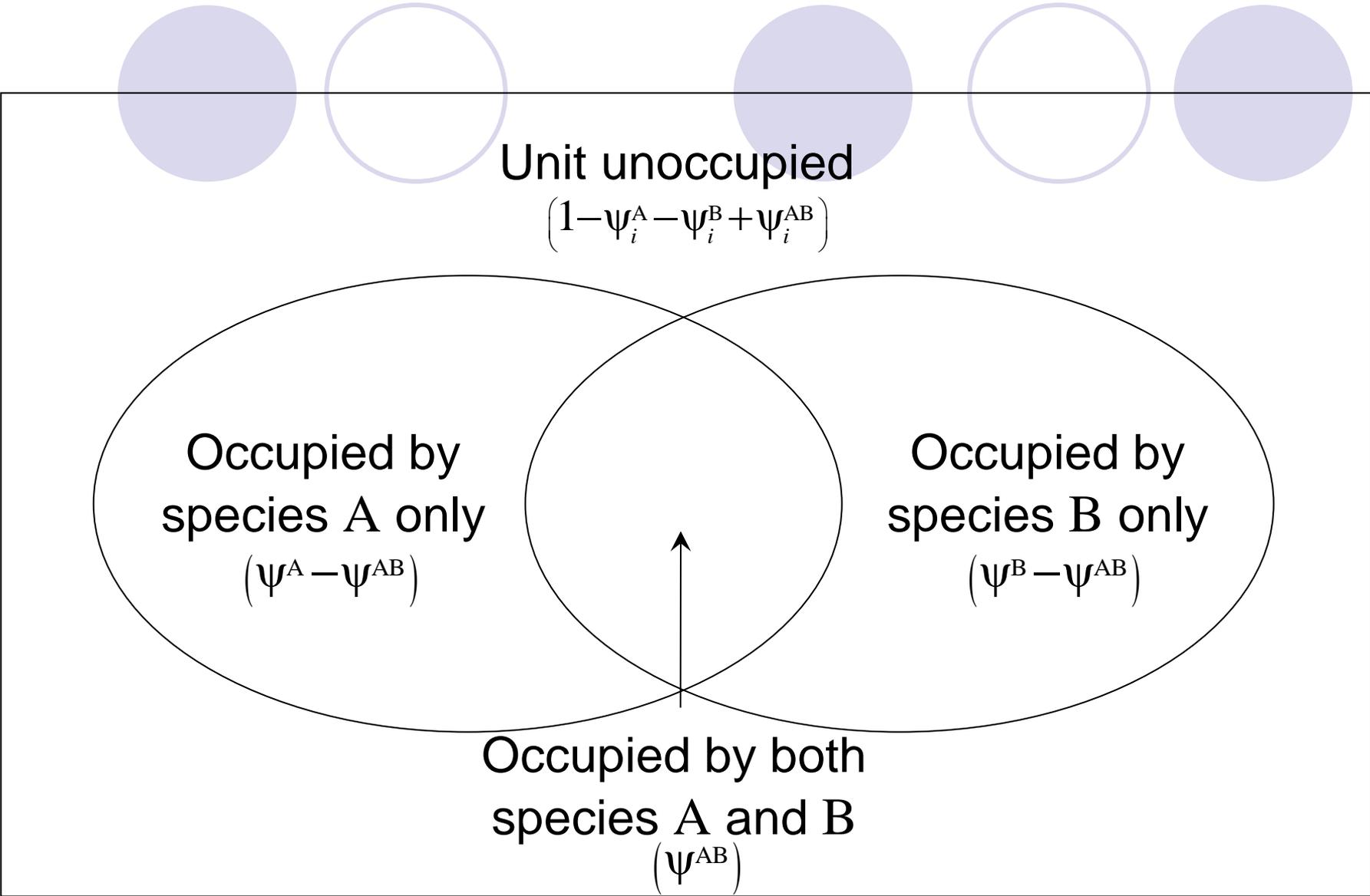
Model parameters



ψ^A = probability unit occupied by species A

ψ^B = probability unit occupied by species B

ψ^{AB} = probability unit occupied by species
A and B



Unit unoccupied

$$(1 - \psi_i^A - \psi_i^B + \psi_i^{AB})$$

Occupied by
species A only

$$(\psi^A - \psi^{AB})$$

Occupied by
species B only

$$(\psi^B - \psi^{AB})$$

Occupied by both
species A and B

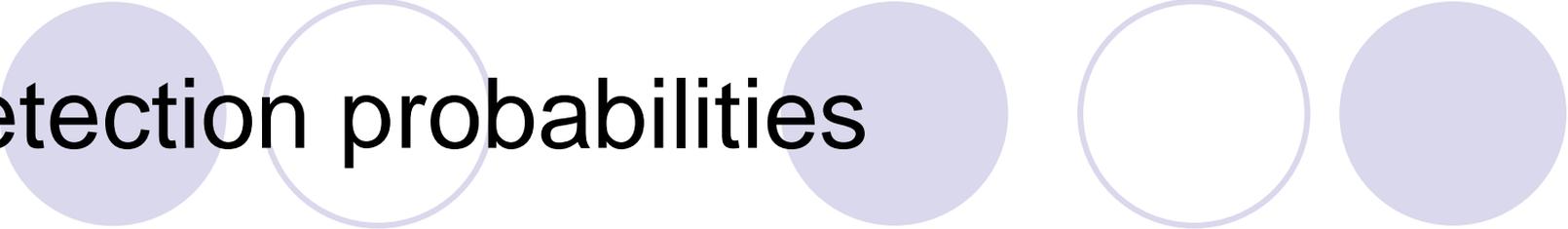
$$(\psi^{AB})$$

Co-occurrence model (multistate)

- Consider units to be in one of 4 mutually exclusive 'states', or more generally 2^l states.
 - occupied by species A and B
 - occupied by species A only
 - occupied by species B only
 - occupied by neither species

$$\phi_0 = \begin{bmatrix} \psi^{AB} & \psi^A - \psi^{AB} & \psi^B - \psi^{AB} & \left(1 - \psi^A - \psi^B + \psi^{AB}\right) \end{bmatrix}$$

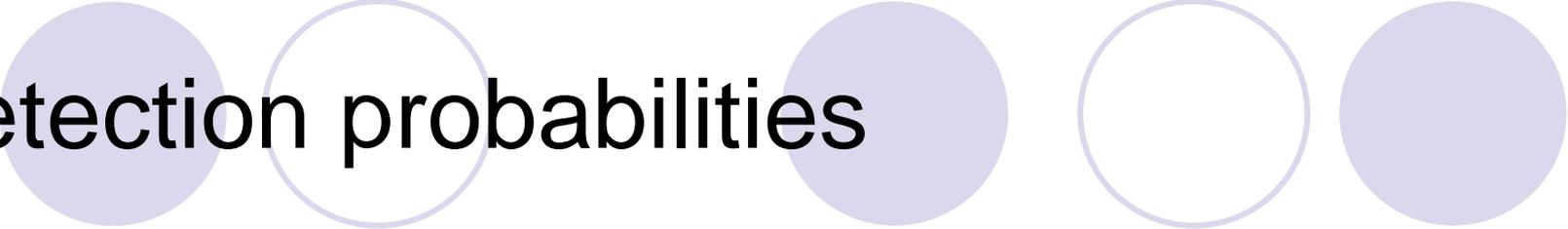
Detection probabilities



Single species only present at site:

p^l = detection probability for species l ,
given only species l is present

Detection probabilities



Both species present at site:

r^{AB} = probability of detecting species A and B

r^{Ab} = probability of detecting species A, but not B

r^{aB} = probability of detecting species B, but not A

r^{ab} = probability of detecting neither species

Detection probabilities

- Define a detection probability vector

$$\mathbf{p}^{\{000\},\{101\}} = \begin{bmatrix} r_1^{\text{aB}} r_2^{\text{ab}} r_3^{\text{aB}} \\ 0 \\ p_1^{\text{B}} (1 - p_2^{\text{B}}) p_3^{\text{B}} \\ 0 \end{bmatrix}$$

Building a two-species model

- Define $\Pr(\mathbf{h}_i^A, \mathbf{h}_i^B)$ for each unit i

$$\Pr(\mathbf{h}_i^A, \mathbf{h}_i^B) = \phi_0 \mathbf{p}^{\{\mathbf{h}_i^A\}, \{\mathbf{h}_i^B\}}$$

- The model likelihood is:

$$L = \prod_{i=1}^s \Pr(\mathbf{h}_i^A, \mathbf{h}_i^B)$$

Building a two-species model

- Consider $\mathbf{h}^A = 11$, $\mathbf{h}^B = 01$
 - Description: Both species present, only species A detected in survey 1, both detected in survey 2
 - Math: $\psi^{AB} r^{Ab} r^{AB}$

Building a two-species model

- Consider $\mathbf{h}^A = 11$, $\mathbf{h}^B = 00$
 - Description: Both species present, only species A detected in either survey,
OR only species A present and was detected in surveys 1 & 2
 - Math: $\psi^{AB} r^{Ab} r^{Ab} + (\psi^A - \psi^{AB}) p^A p^A$

Building a two-species model

- Consider $\mathbf{h}^A = 00$, $\mathbf{h}^B = 00$
 - Description: Both species present with neither ever being detected,
OR only species A present and never detected,
OR only species B present and never detected,
OR both species absent
 - Math: $\psi^{AB} (r^{ab})^2 + (\psi^A - \psi^{AB})(1 - p^A)^2 + (\psi^B - \psi^{AB})(1 - p^B)^2 + (1 - \psi^A - \psi^B + \psi^{AB})$

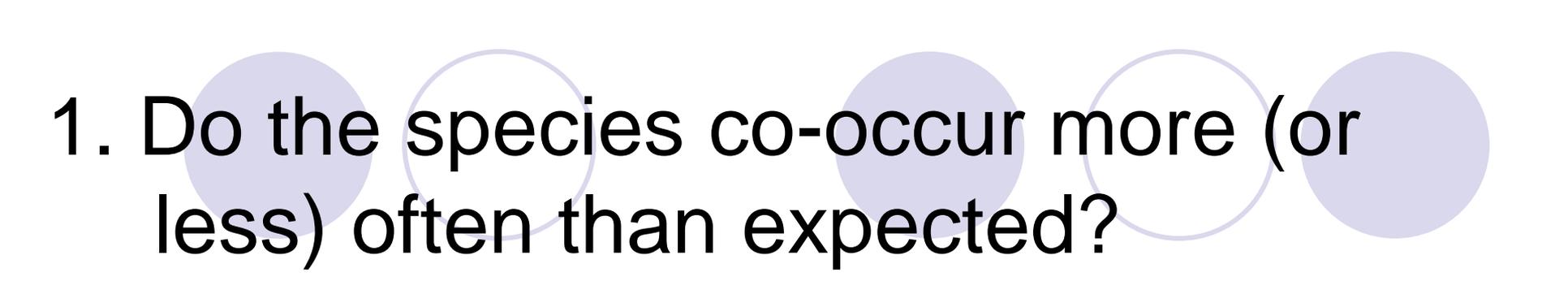
1. Do the species co-occur more (or less) often than expected?

- If species occur at units independently then,

$$\psi^{AB} = \psi^A \times \psi^B$$

- The level of co-occurrence could be quantified as,

$$\hat{\phi} = \frac{\hat{\psi}^{AB}}{\hat{\psi}^A \times \hat{\psi}^B}$$



1. Do the species co-occur more (or less) often than expected?

- Suggested reparameterization,

$$\psi^{AB} = \psi^A \times \psi^B \times \varphi$$

- Model φ directly

1. Do the species co-occur more (or less) often than expected?

- Another parameterization,

$$\psi^{AB} = \psi^{B|A} \psi^A$$

$$\psi^B = \psi^{B|A} \psi^A + \psi^{B|a} (1 - \psi^A)$$

- Estimated parameters are ψ^A , $\psi^{B|a}$ and $\psi^{B|A}$.

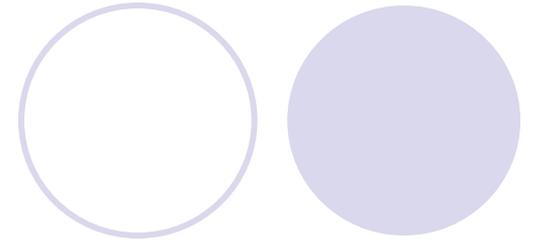
1. Do the species co-occur more (or less) often than expected?

- A third parameterization,

$$v = \frac{\psi^{B|A} / (\psi^A - \psi^{B|A})}{\psi^{B|a} / (1 - \psi^A - \psi^{B|a})}$$

- Equivalent to logistic regression with the presence of sp. A as a predictor variable for the presence of sp. B
- Estimated parameters are ψ^A , $\psi^{B|a}$ and v (other sets possible).

2. Are the species detected independently?



- Redefine $r^{AB} = r^A \times r^B \times \delta$
- Detections are independent if, $\delta = 1$
- Or use similar reparameterizations as for occupancy

3. Is the probability of detecting species A affected by the presence of species B?

- Consider models with the constraint,

$$r^A = p^A$$

- Or similarly, $r^B = p^B$

Multiple-season species co-occurrence

- Single-season model only allows inference about the *patterns* of co-occurrence.
- To make inferences about the *dynamic processes* of change in co-occurrence need to survey the species at systematic points in time.
- Dynamic processes are probabilities of colonization and local extinction, given the presence or absence of other species.
- These processes *produce* observed patterns.

Multiple-season species co-occurrence

- Define a matrix that determines how the occupancy state of units may change between seasons t and $t+1$.

$$\phi_t = \begin{bmatrix} AB \rightarrow AB & AB \rightarrow A & AB \rightarrow B & AB \rightarrow U \\ A \rightarrow AB & A \rightarrow A & A \rightarrow B & A \rightarrow U \\ B \rightarrow AB & B \rightarrow A & B \rightarrow B & B \rightarrow U \\ U \rightarrow AB & U \rightarrow A & U \rightarrow B & U \rightarrow U \end{bmatrix}$$

Multiple-season species co-occurrence

- Define a matrix that determines how the occupancy state of units may change between seasons t and $t+1$.

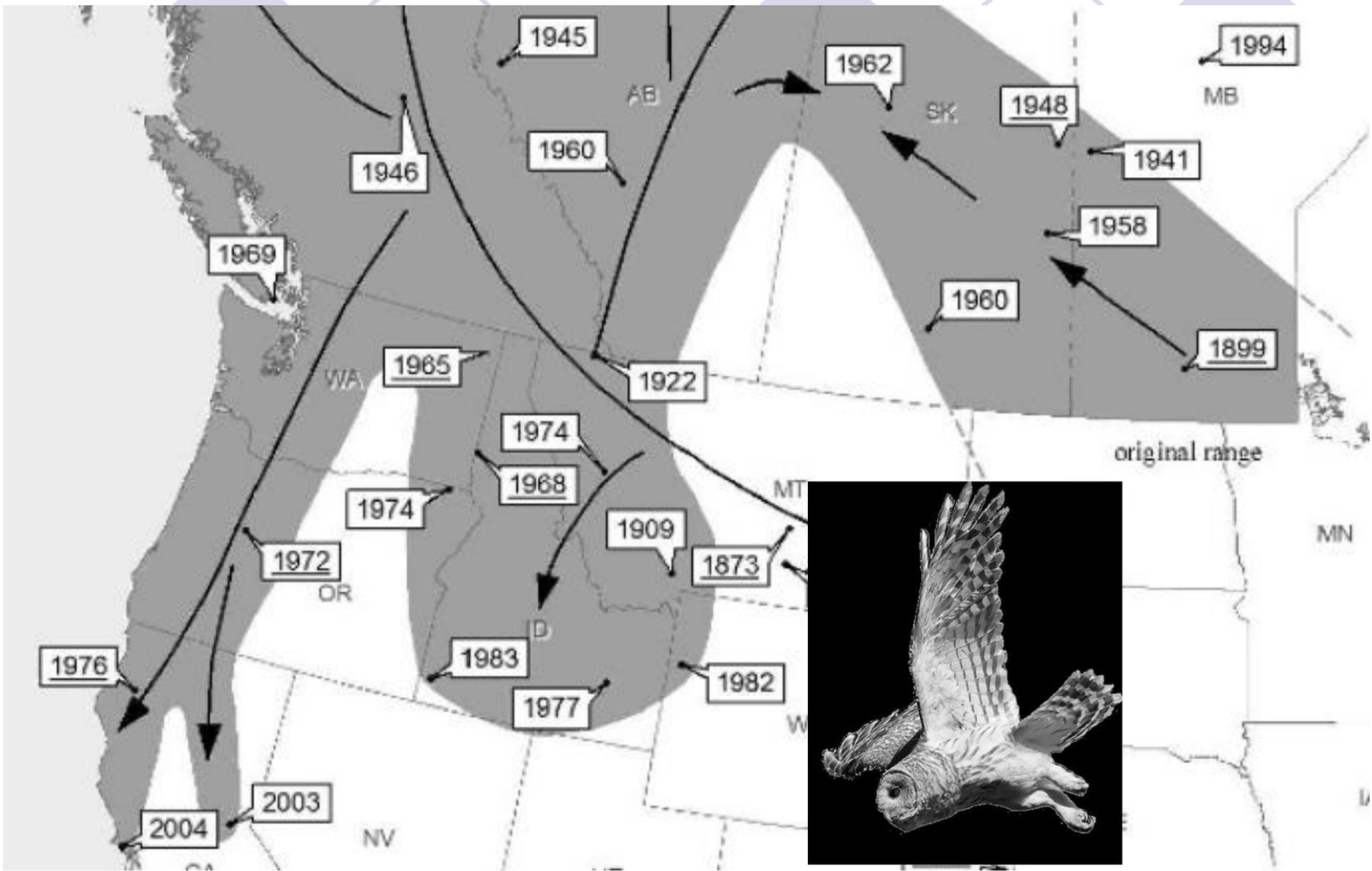
$$\phi_t = \begin{bmatrix} 1 - \varepsilon_t^A - \varepsilon_t^B + \varepsilon_t^{AB} & \varepsilon_t^B - \varepsilon_t^{AB} & \varepsilon_t^A - \varepsilon_t^{AB} & \varepsilon_t^{AB} \\ \eta_t^B & 1 - \omega_t^{AB} - \eta_t^B - \nu_t^A & \omega_t^{AB} & \nu_t^A \\ \eta_t^A & \omega_t^{BA} & 1 - \omega_t^{BA} - \eta_t^A - \nu_t^B & \nu_t^B \\ \gamma_t^{AB} & \gamma_t^A - \gamma_t^{AB} & \gamma_t^B - \gamma_t^{AB} & 1 - \gamma_t^A - \gamma_t^B + \gamma_t^{AB} \end{bmatrix}$$

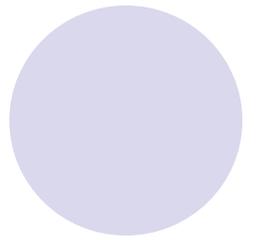
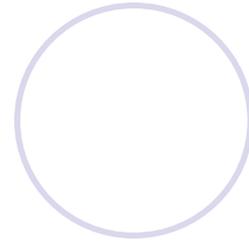
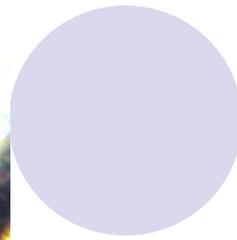
Multiple-season species co-occurrence

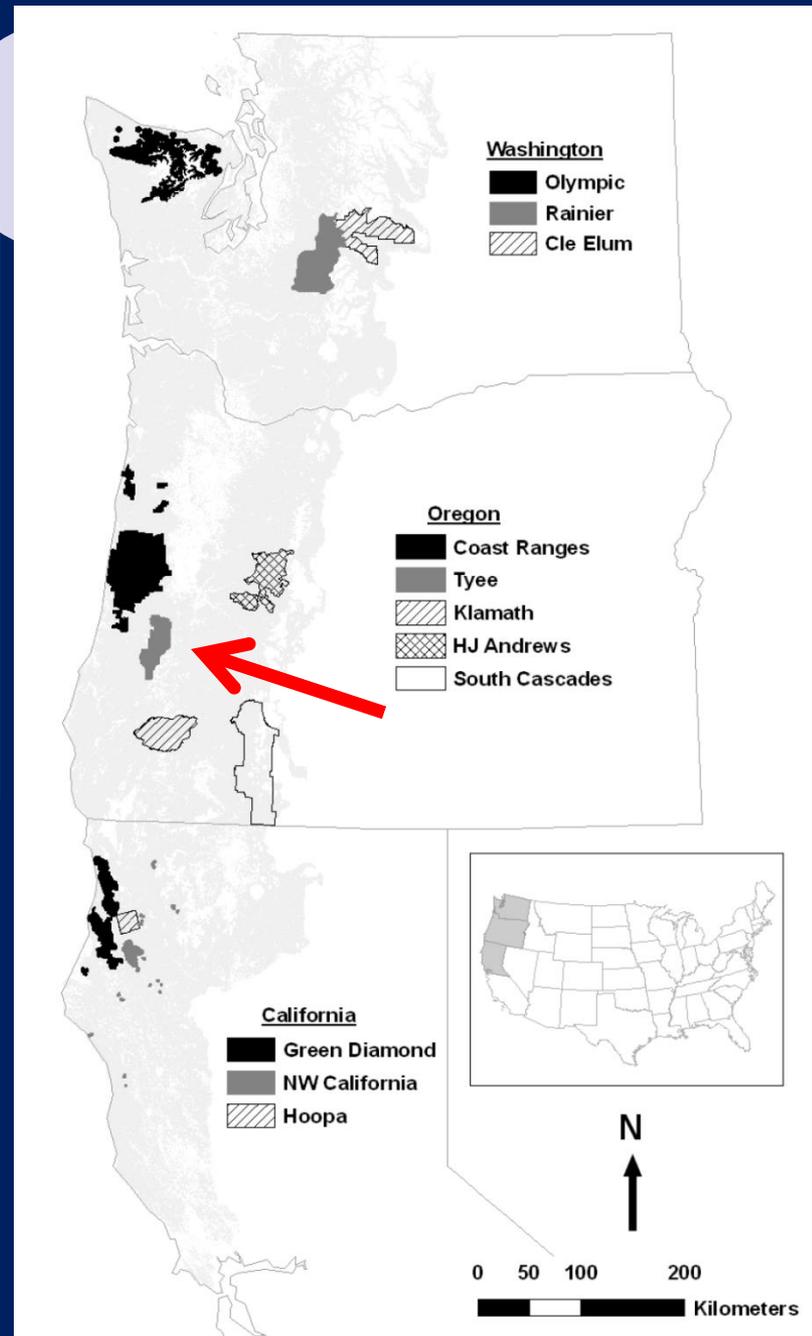
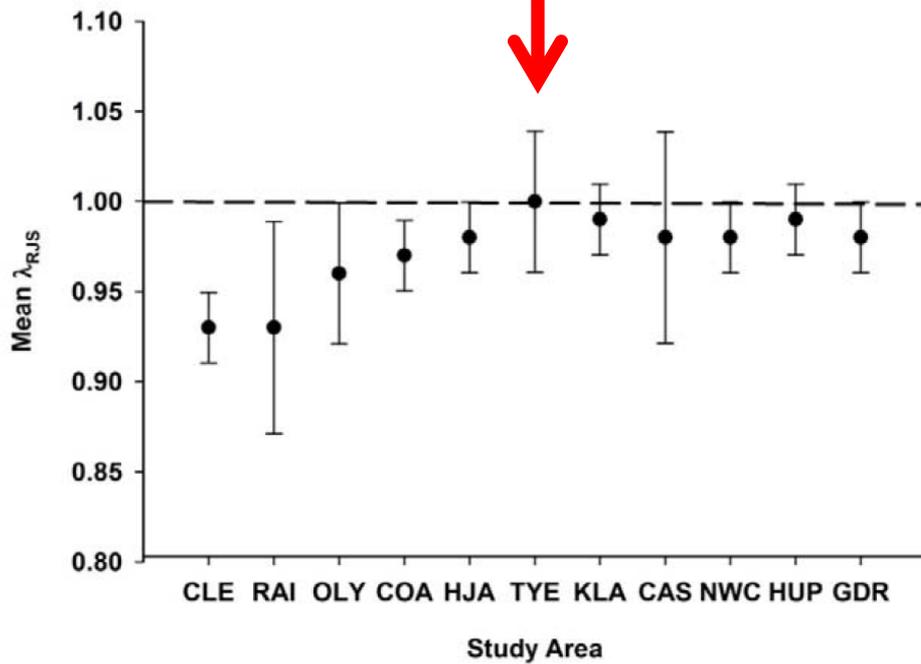
- Observed data likelihood approach:

$$\Pr(\mathbf{h}_i^A, \mathbf{h}_i^B) = \phi_0 \prod_{t=1}^{T-1} D\left(\mathbf{p}_t^{\{\mathbf{h}_{it}^A, \mathbf{h}_{it}^B\}}\right) \phi_t \mathbf{p}_T^{\{\mathbf{h}_{it}^A, \mathbf{h}_{it}^B\}}$$

- Complete data likelihood could also be developed and used with EM algorithm or data augmentation







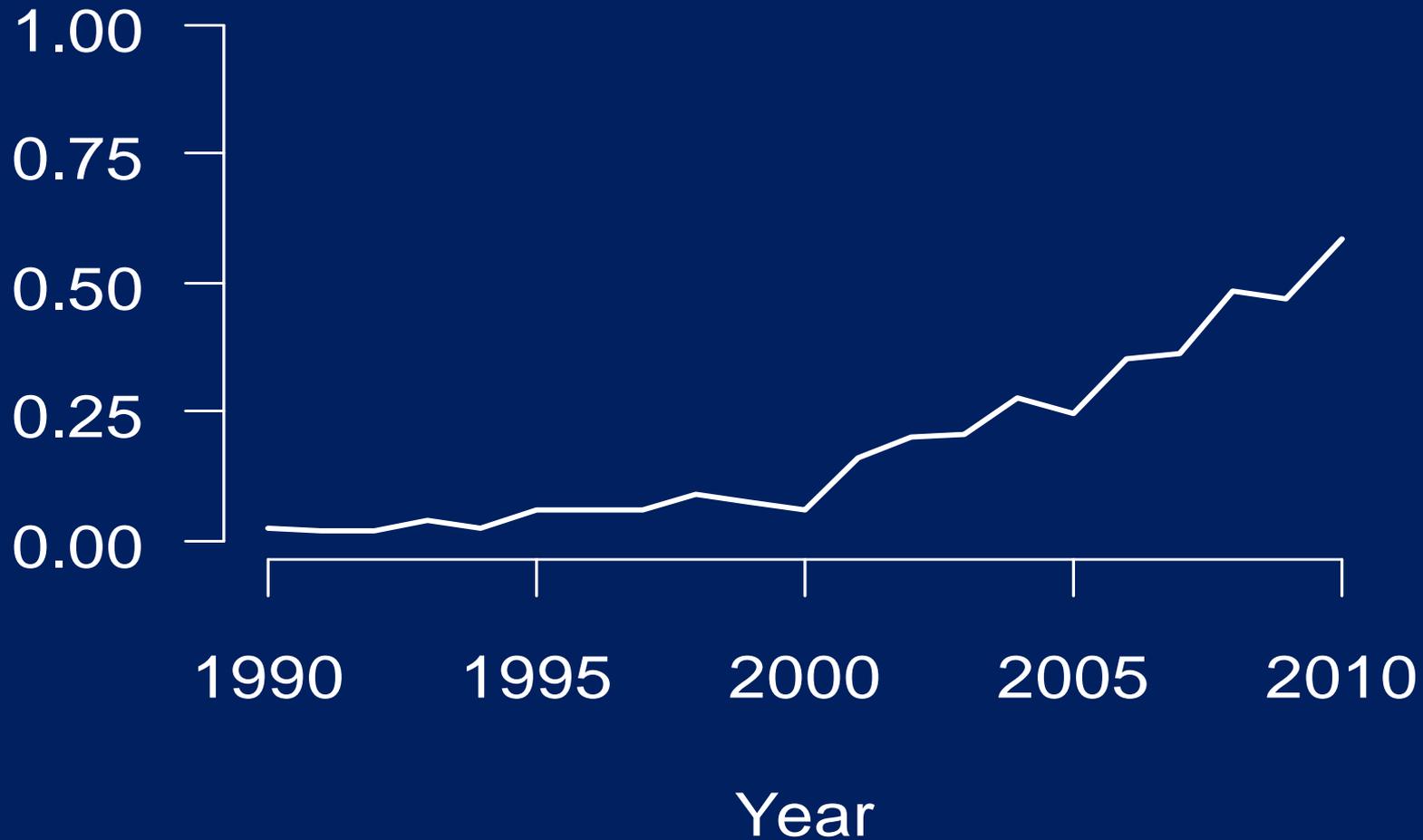
North

South



Forsman et al. (2011)
Population demography
of Northern spotted owl

Proportion of sites with barred owl detections



Detection (Bailey et al. 2009)



- Northern spotted owl
 - Time of day, method, barred owl presence
 - 0.05 – 0.57



- Barred owl
 - Time of day, method
 - Survey length or Northern spotted owl presence
 - 0.03 – 0.46

Multispecies dynamic model: Inferences and questions

- Detection
 - Is barred owl detection lower in jointly occupied territories for biological or methodological reasons?
- Species interactions
 - Is competition completely unidirectional?
 - What is the strength of competition (effect size)?
- Forest type
 - BO like riparian forest.
 - NSO like older growth forest.
 - Does this biological difference create a mechanism for coexistence?
- Forecast occupancy dynamics
 - Will Northern spotted owls persist at Tyee?

Multispecies dynamic model

- Detection

- Is barred owl detection lower in jointly occupied territories for biological or methodological reasons?

- Previous result (Bailey et al. 2009)

- BO showed lower detection probabilities when NSO was present

- Current analysis

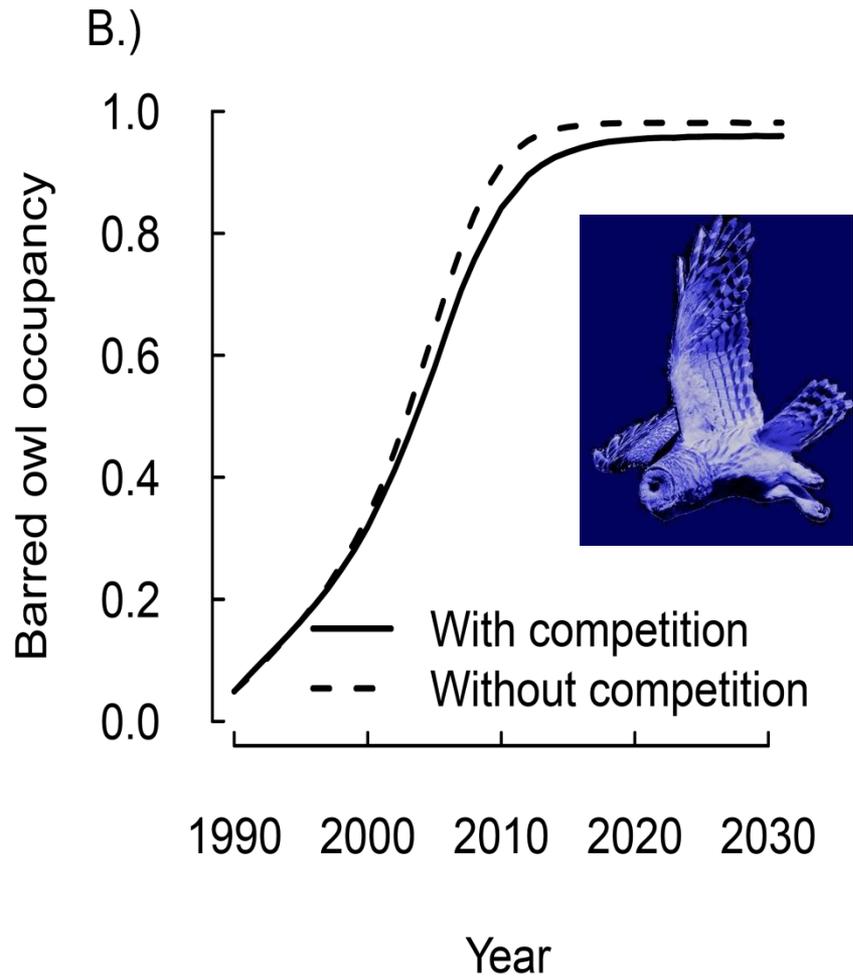
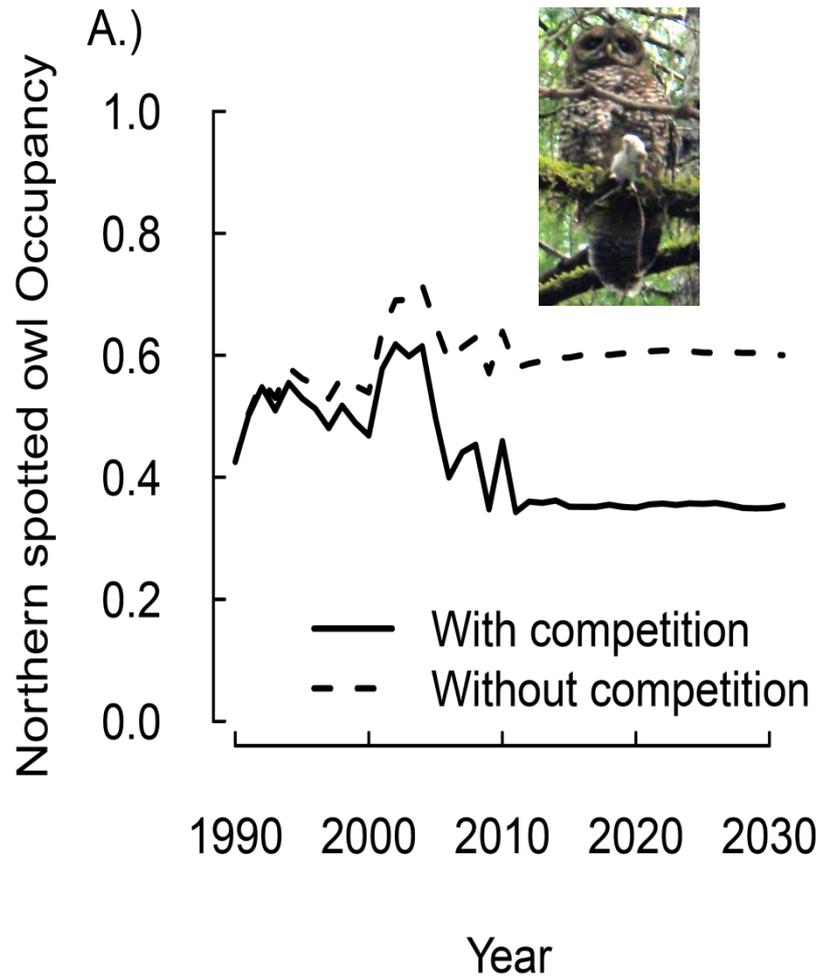
- strong evidence that survey length influenced BO detection

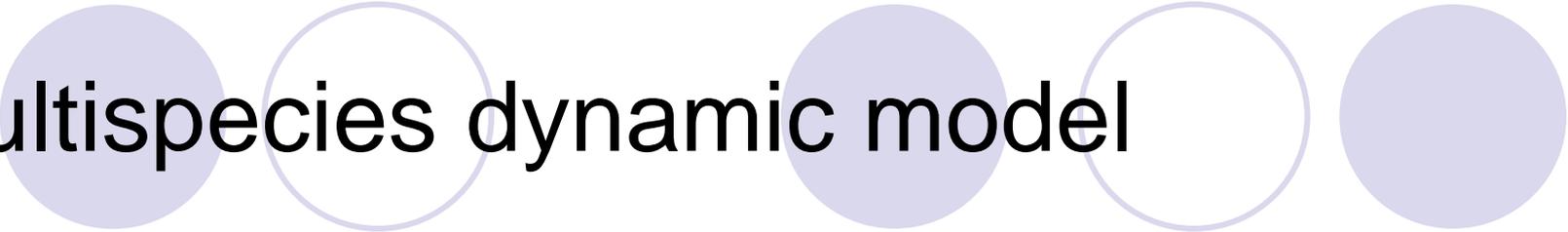
- evidence is motivating change in survey protocol

Multispecies dynamic model

- Species interactions
 - Is competition completely unidirectional?
 - What is the strength of competition (effect size)?
- Extinction probability
 - Higher each species when other species is present
 - Much larger effect of BO on NSO than vice versa
- Colonization
 - Some evidence of lower NSO colonization of patches inhabited by BO
 - Some evidence of higher BO colonization of patches inhabited by NSO

Species interactions

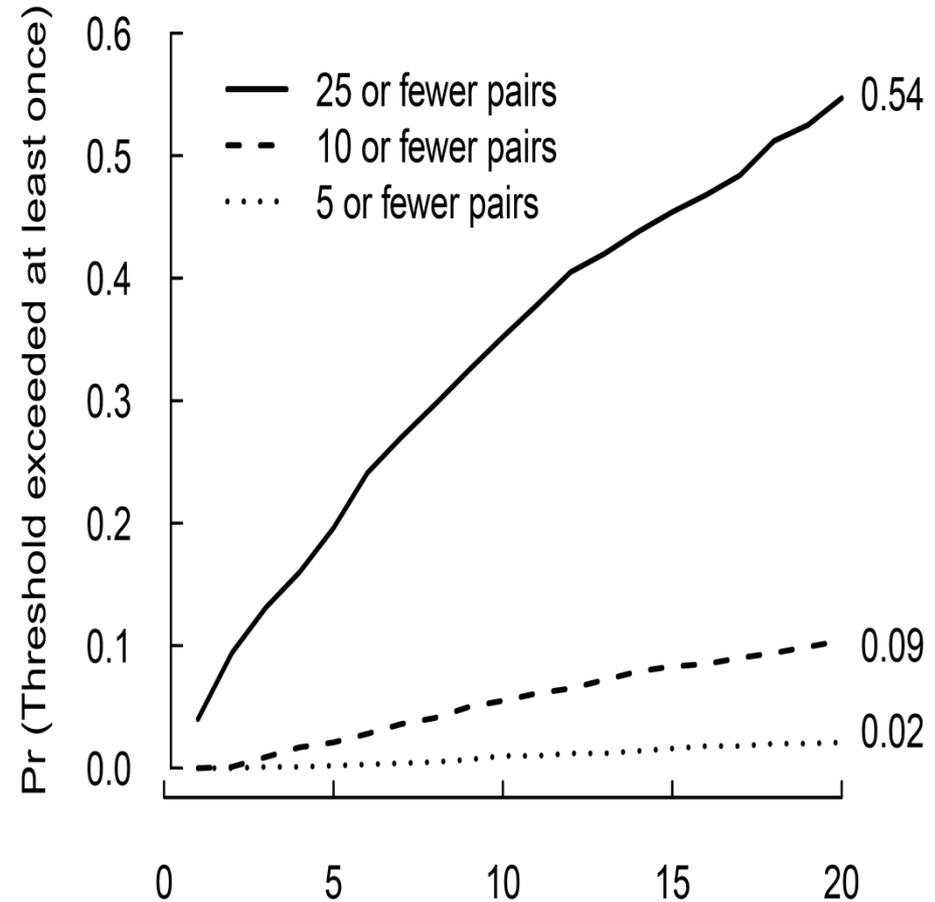
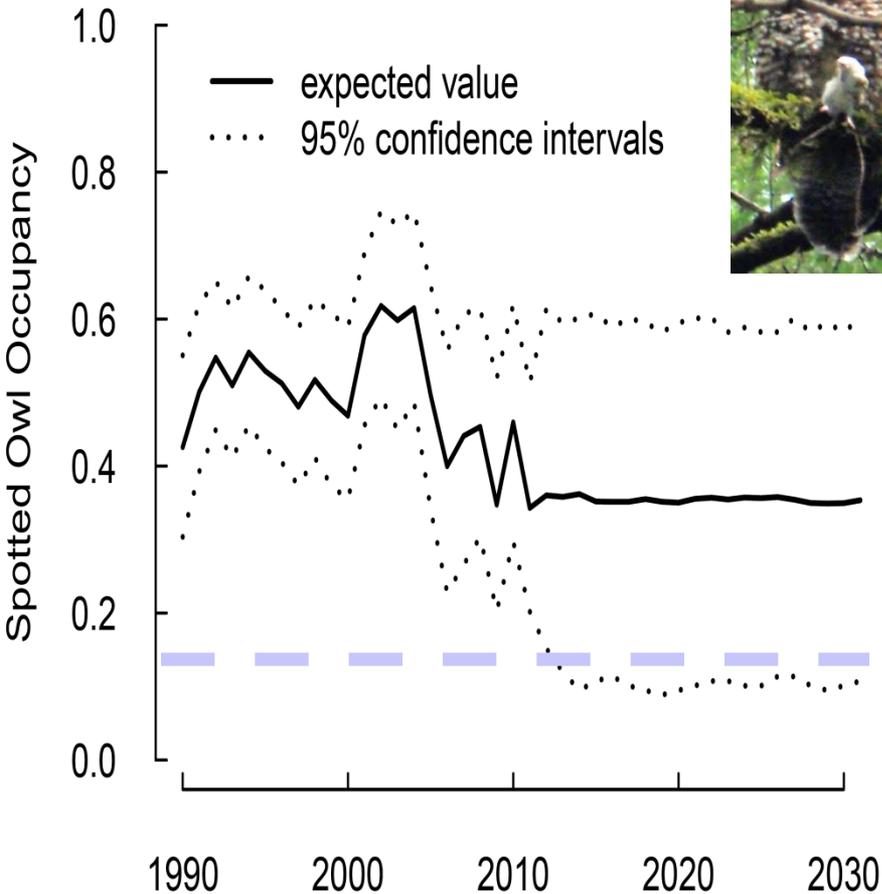




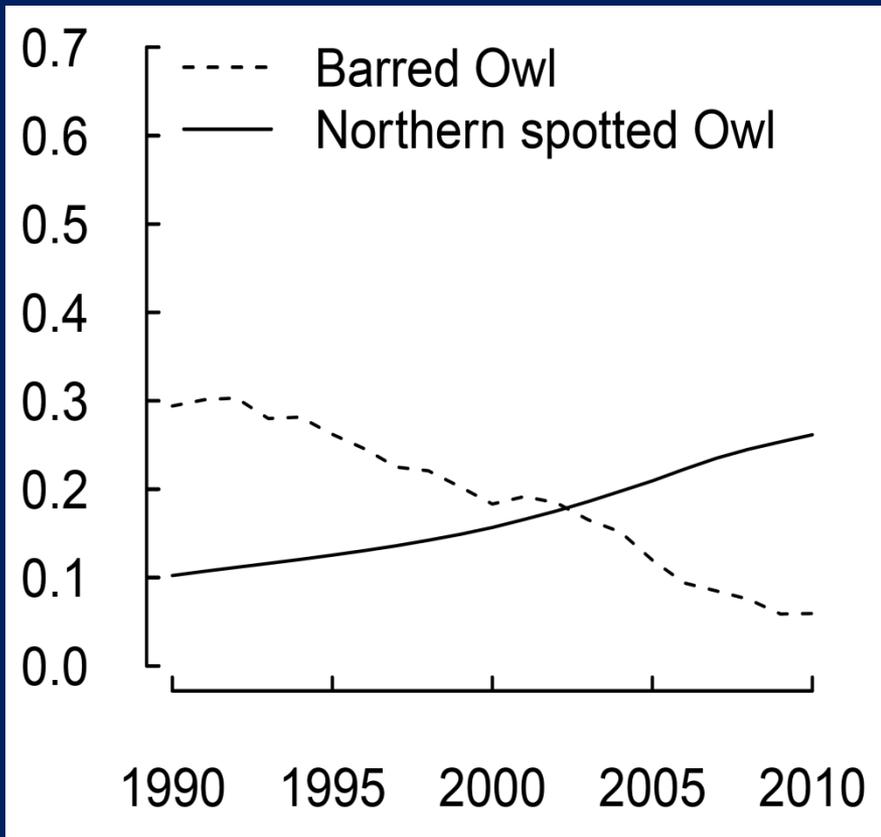
Multispecies dynamic model

- Forecast occupancy dynamics
 - Will Northern spotted owls persist at Tyee?
- Uncertain, but not optimistic
 - Simulations/projections indicate NSO persistence on average
 - But NSO occupancy occasionally drops very low
 - “The future’s uncertain and the end is always near” (Doors/Morrison 1970)

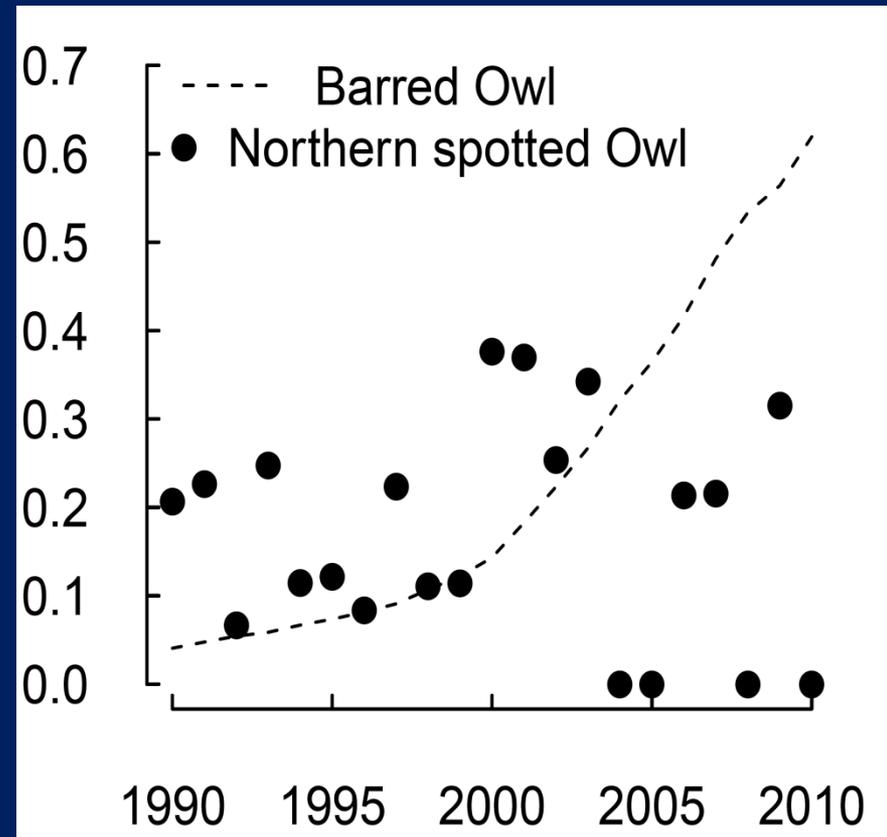
Northern spotted owl persistence?



Population dynamics and uncertainty



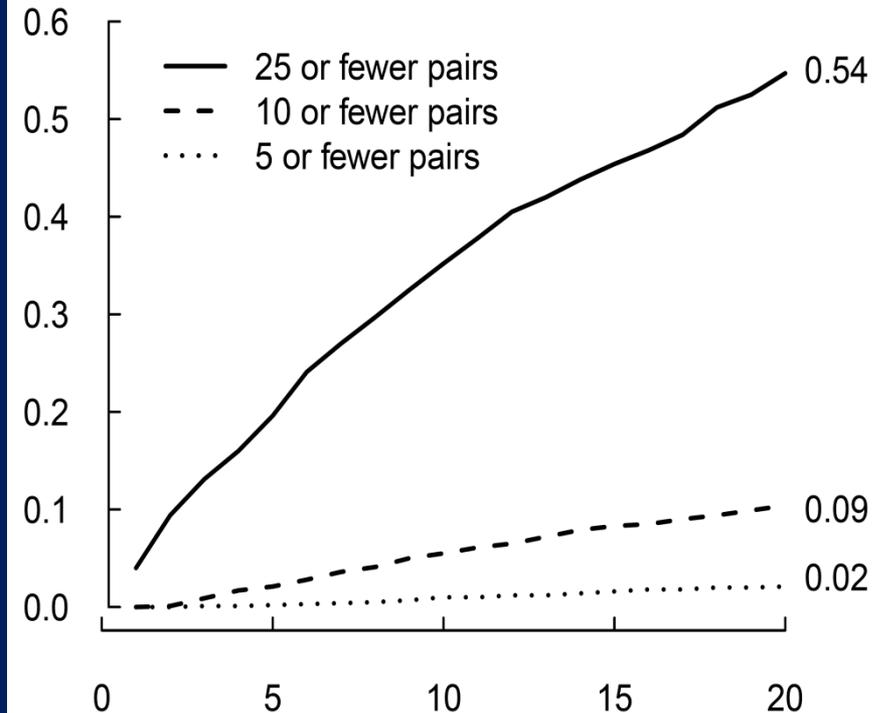
NSO extinction rates will remain high.



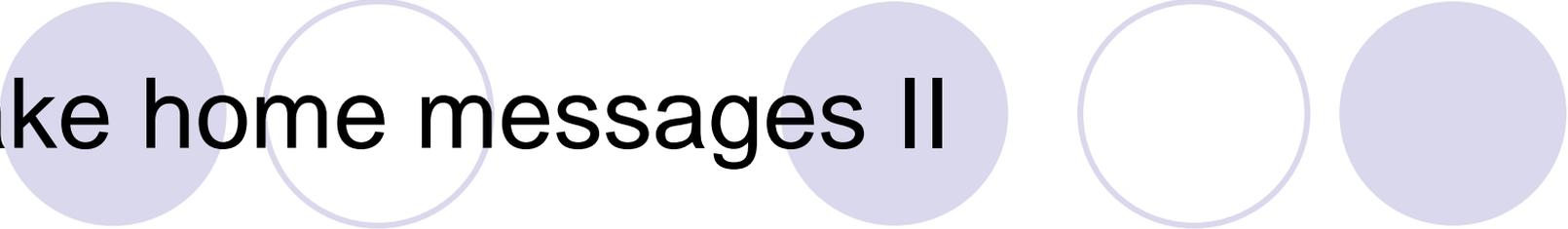
Will colonization eventually decline?

Take home messages I

- Dynamic modeling provides means of making inferences and projections (with and without management)
- Could add dynamic habitat modeling
- Autologistic modeling useful for BO invasion

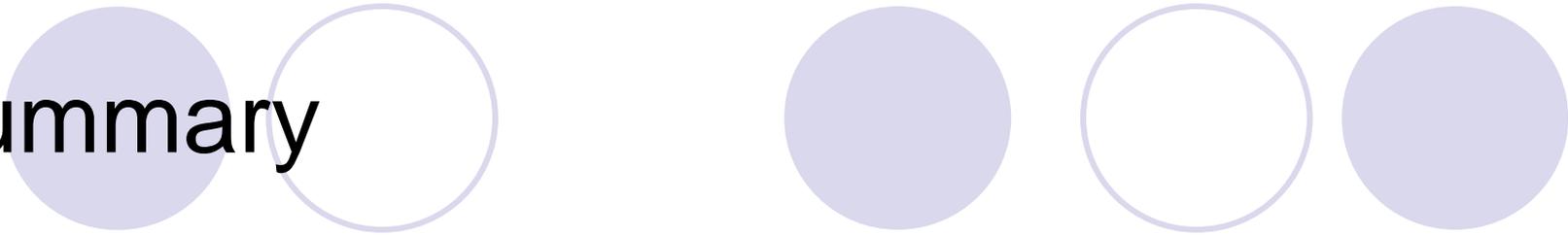


Take home messages II



- Evidence for macroecological effects of competition: asymmetric competition with BO may be a factor associated with decreases in NSO occupancy
- Dynamic model projections indicate attainment of dynamic equilibrium for NSO, but with non-negligible probabilities of drops to very low levels of occupancy
- Dynamic model can be useful in projecting effects of various management options (e.g., BO removal)

Summary



- Imperfect detection of species may lead to misleading conclusions about species co-occurrence.
- Similarly, some apparent relationships may be explained by different habitat preferences or different responses to environmental changes.
- Reliable inferences about change can only be made by observing the system at systematic points in time.