

# Introduction to distribution and abundance



Marc Kéry  
Swiss Ornithological Institute  
[marc.kery@vogelwarte.ch](mailto:marc.kery@vogelwarte.ch)

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## Contents

- Why do we care about distribution and abundance ?
- What is occurrence/distribution ?
- The ugly truth about all distribution & abundance data
- Kinds of data on distribution and abundance
- Value of hierarchical models for ecological data



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- **Why do we care about distribution and abundance ?**
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**Why do we care about distribution and abundance ?**



Why do we care about distribution and abundance ?

# HUGE TOPICS !!!

- Population central concept in ecology and management
- Population size (N) first descriptor of the population
- Population size single-most important “thing” in ecology and management
- Distribution almost as important ...  
.... or more (e.g., cheaper data, simpler models)
- “Ecology = Study of distribution and abundance” (e.g., textbook by Krebs)
- though see later about relationship between the two



Why do we care about distribution and abundance ?

# HUGE TOPICS !!!

- Interest for distribution:
  - Species distribution modeling industry
  - Metapopulation ecology
  - Climate change
  - Disease ecology/disease surveillance
  - Invasive species
  - Niche ecology



## Relationship between distribution and abundance

- Distribution and abundance sometimes treated as separate quantities
- e.g., zero-inflated Poisson modeling of occurrence and of abundance, given occurrence
- Model for occurrence/distribution at site  $i$ :

$$z_i \sim \text{Bernoulli}(\psi_i)$$
$$\text{logit}(\psi_i) = \alpha_0 + \alpha_1 * Xi + \dots$$

- Model for abundance at site  $i$ , given occurrence (i.e.,  $z_i = 1$ ):

$$N_i \sim \text{Poisson}(z_i * \lambda_i)$$
$$\text{log}(\lambda_i) = \beta_0 + \beta_1 * Xi + \beta_2 * W_i$$

- That does not, or very rarely, make sense !

Why ?



## Relationship between distribution and abundance

- **Because it's the same thing !**
- As if modeling height of people in two steps:
  - 1<sup>st</sup> model: probability of being  $>Y_0$  cm (e.g.,  $Y_0 = 150$  cm)
  - 2<sup>nd</sup> model: truncated Normal for  $Y$ , given  $>150$  cm
- Let's look at the relationship between occurrence, distribution and abundance in more detail ...



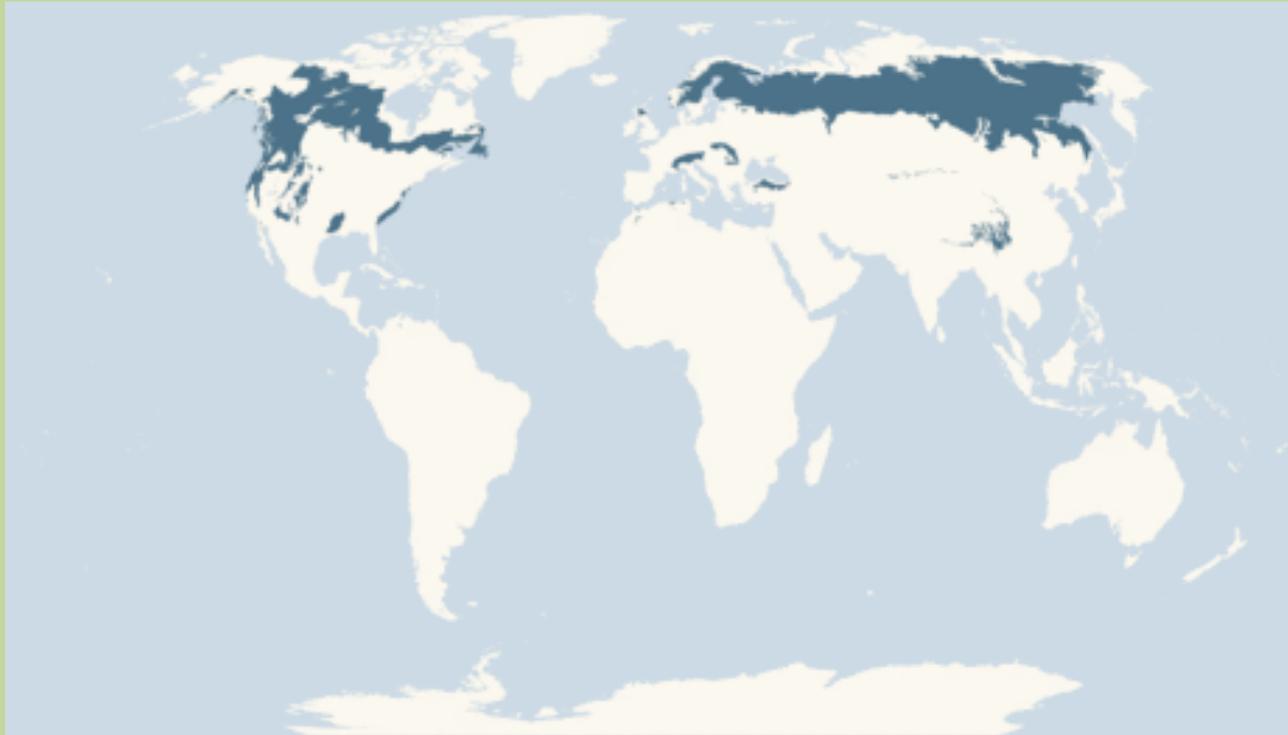
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## What is occurrence / (species) distribution ?

- Google “common crossbill distribution”
- We immediately understand what this means ...



[http://www.bbc.co.uk/nature/life/Common\\_Crossbill](http://www.bbc.co.uk/nature/life/Common_Crossbill)



## What is occurrence / (species) distribution ?

- Or do we really ??? What **exactly** is meant by that picture ?



# What is occurrence / distribution ?

- What **exactly** is meant by such distribution maps ?



Male crossbill



Study area

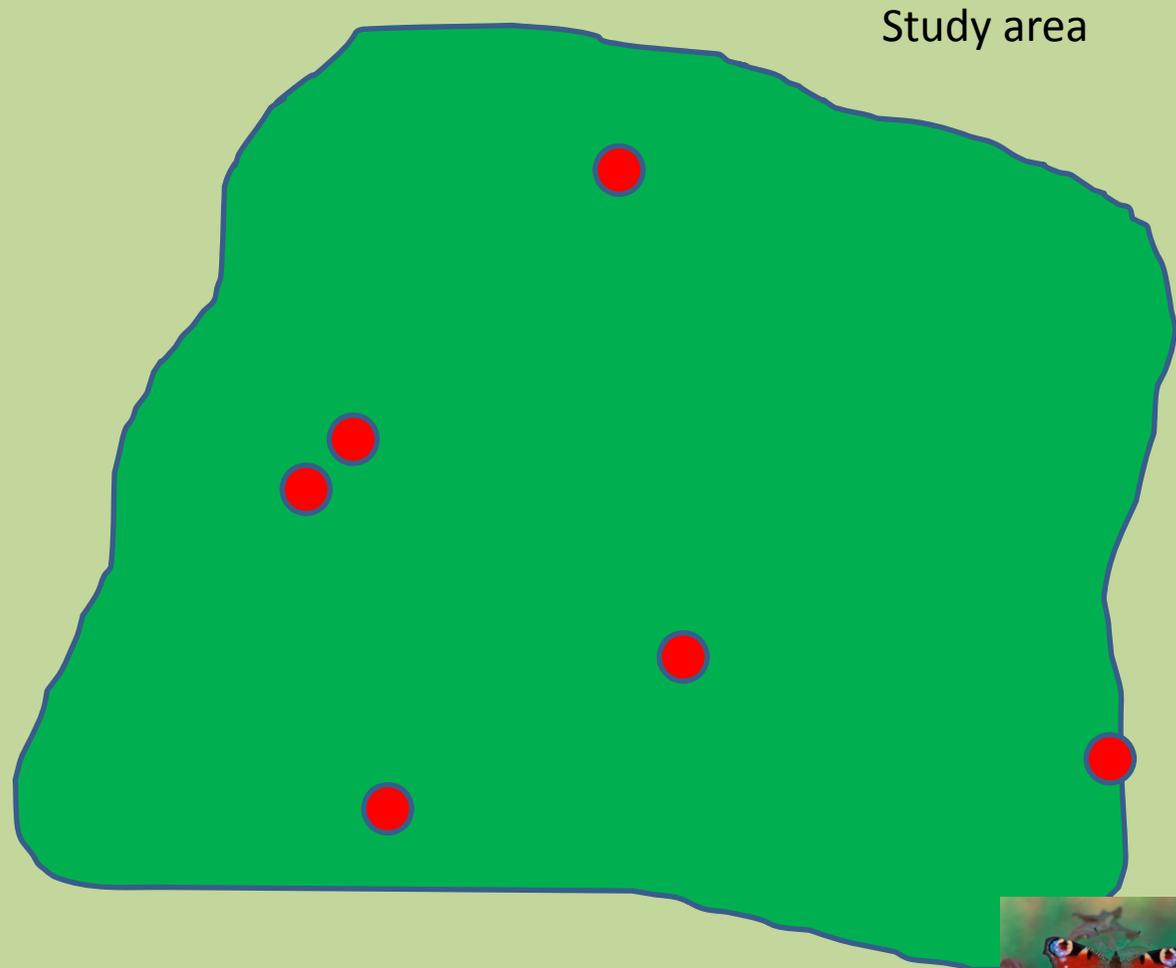


# What is occurrence / distribution ?

- What **exactly** is meant by such distribution maps ?



Male crossbill



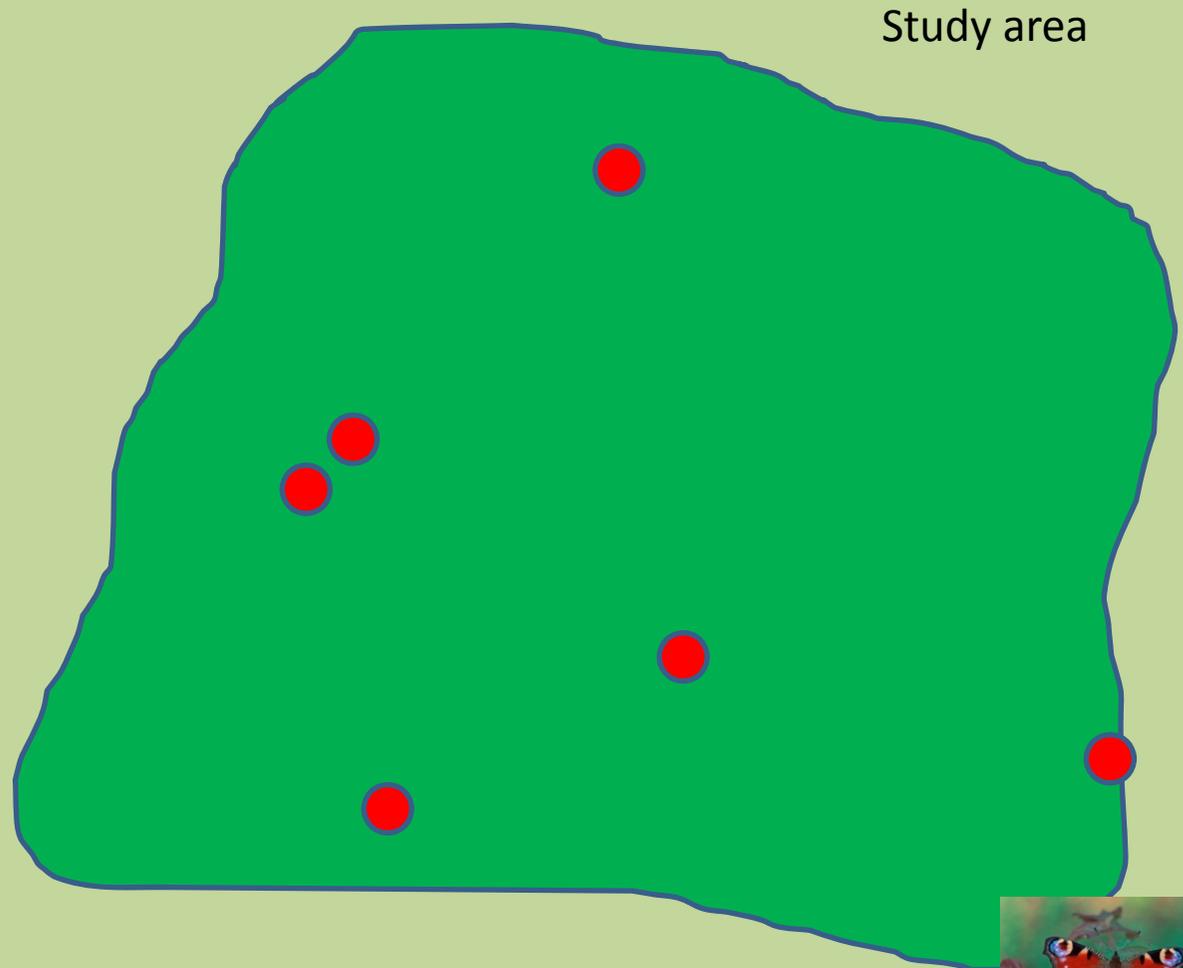
Study area



## What is occurrence / distribution ?

- **Distribution:** “area where a species occurs”

$$\frac{\textit{Area with crossbill}}{\textit{Total area}}$$

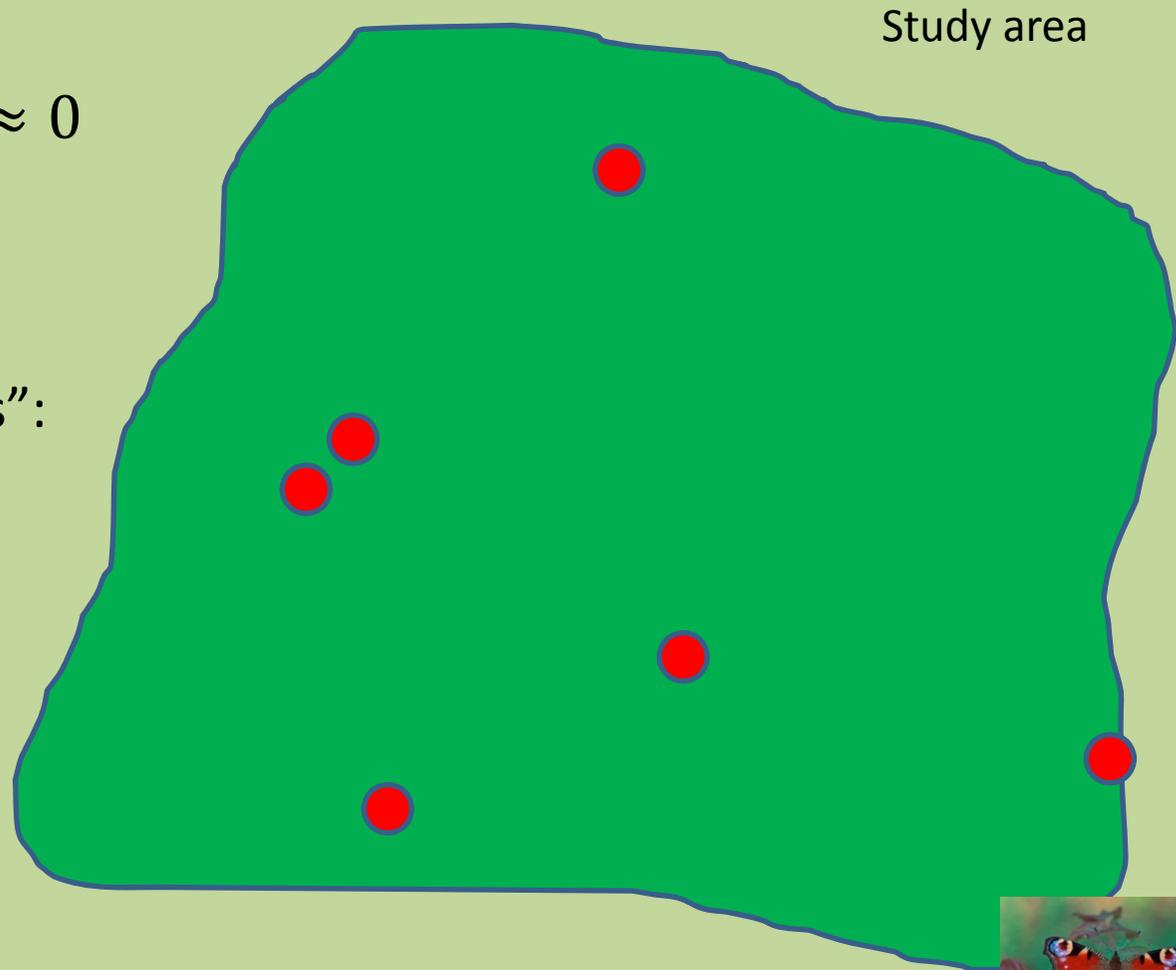


# What is occurrence / distribution ?

- **Distribution:** “area where a species occurs”

$$\frac{\textit{Area with crossbill}}{\textit{Total area}} \approx 0$$

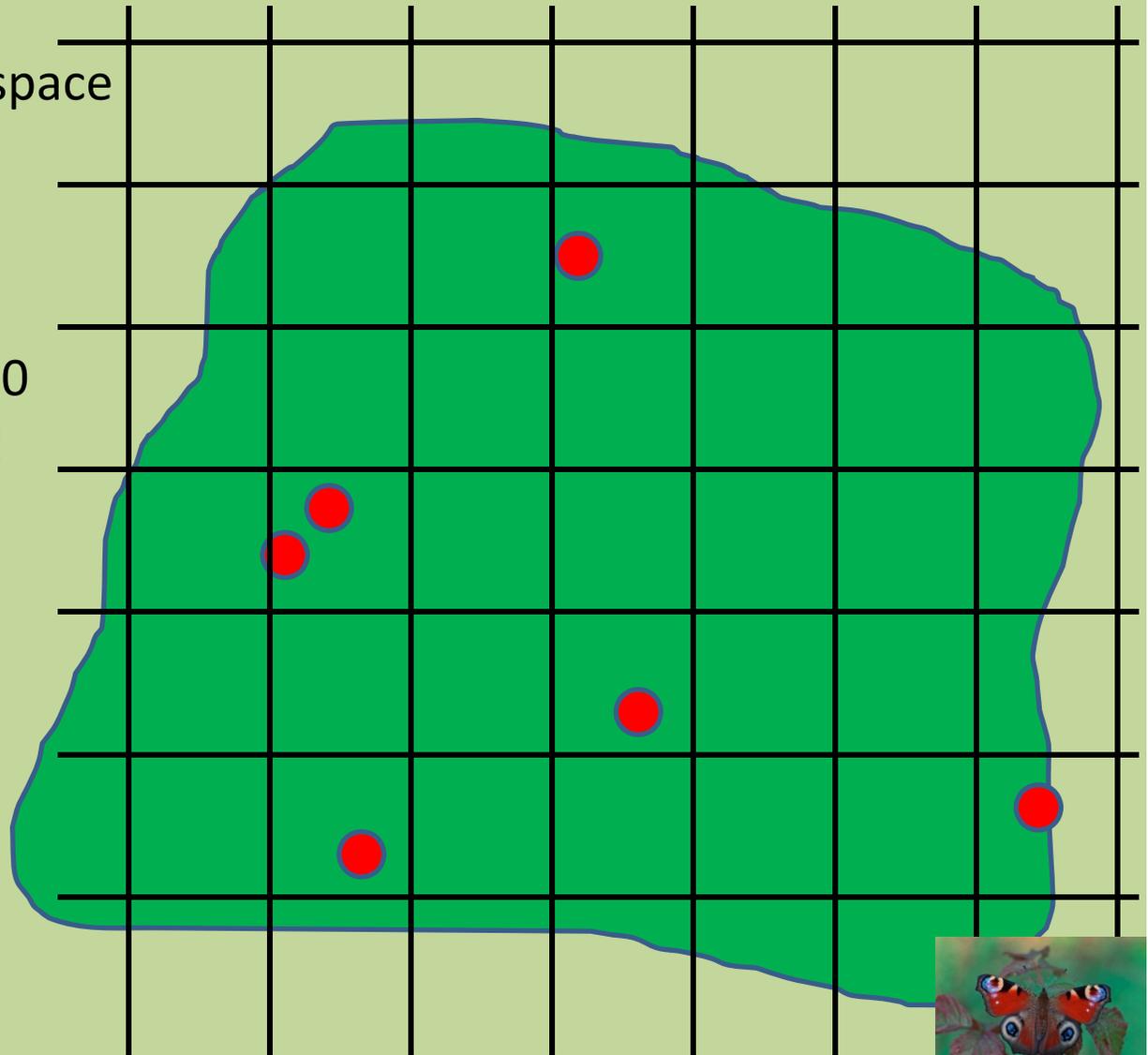
- Birds small & discrete
- Approximately “points”:
- Spatial point pattern: realization of spatial point process



## What is occurrence / distribution ?

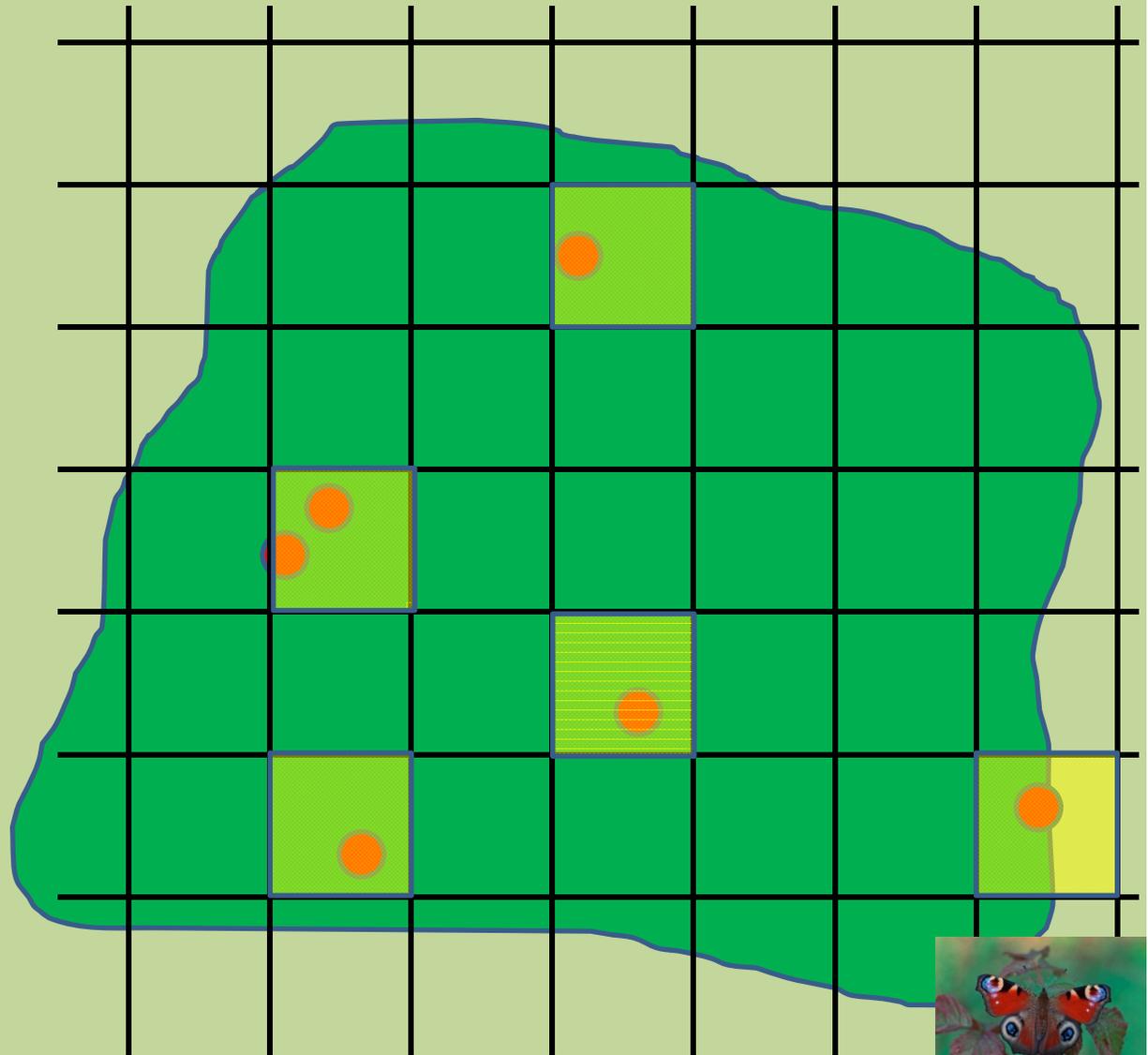
- In practice (\*), most often discretize space
- e.g., impose grid and summarize spatial point process
- Otherwise bird area = 0 (and distribution = 0) !

(\*) spatial point patterns *can* be modelled directly, but may be difficult, analyses/software not well-known, data inadequate, hard to accommodate imperfect detection ...



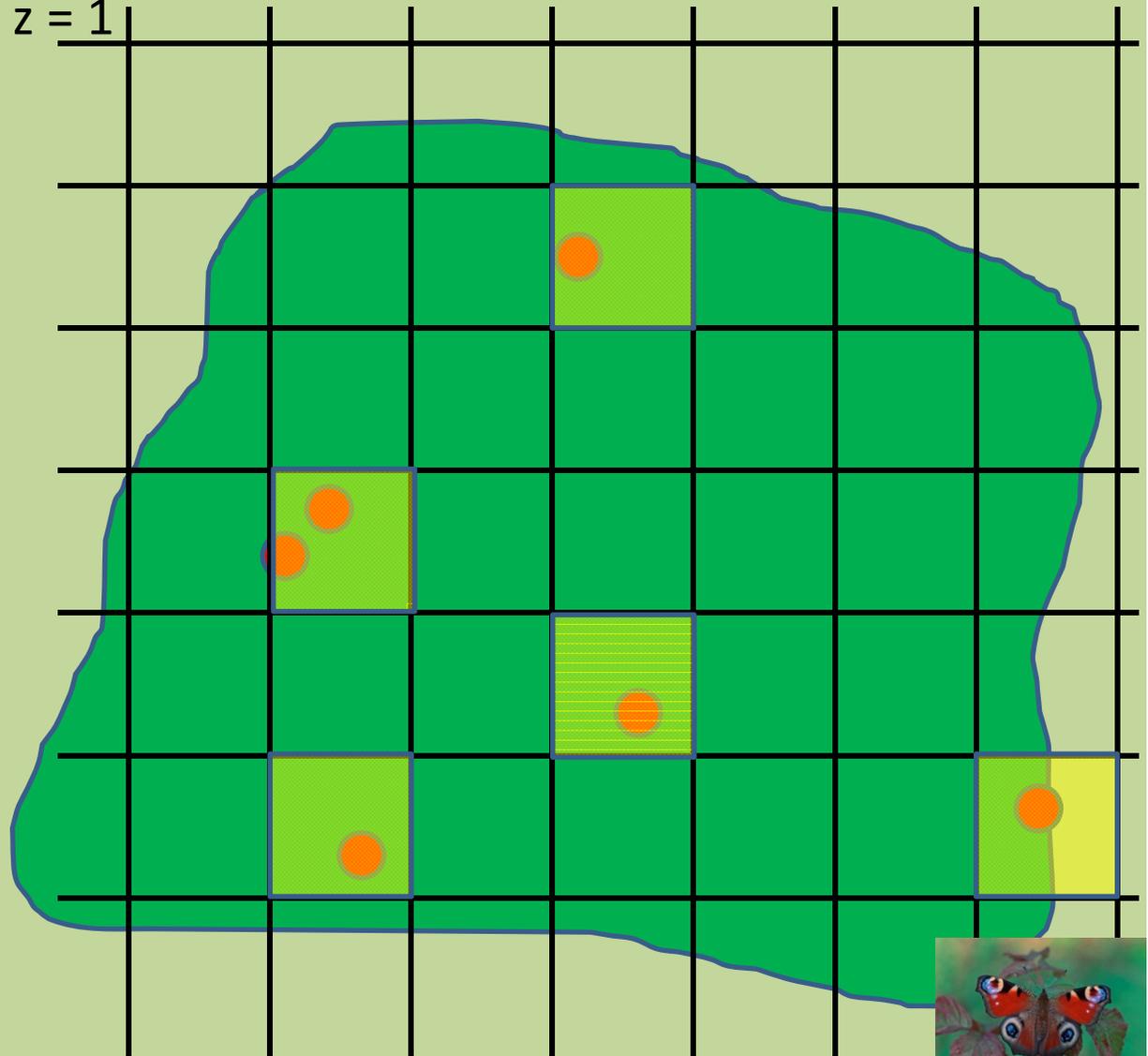
## What is occurrence / distribution ?

- Occurrence (z):  
areal summary  
of pixel abundance N
- Distribution:  
pattern of z,  
sum of occurrences  
(5 pixels)



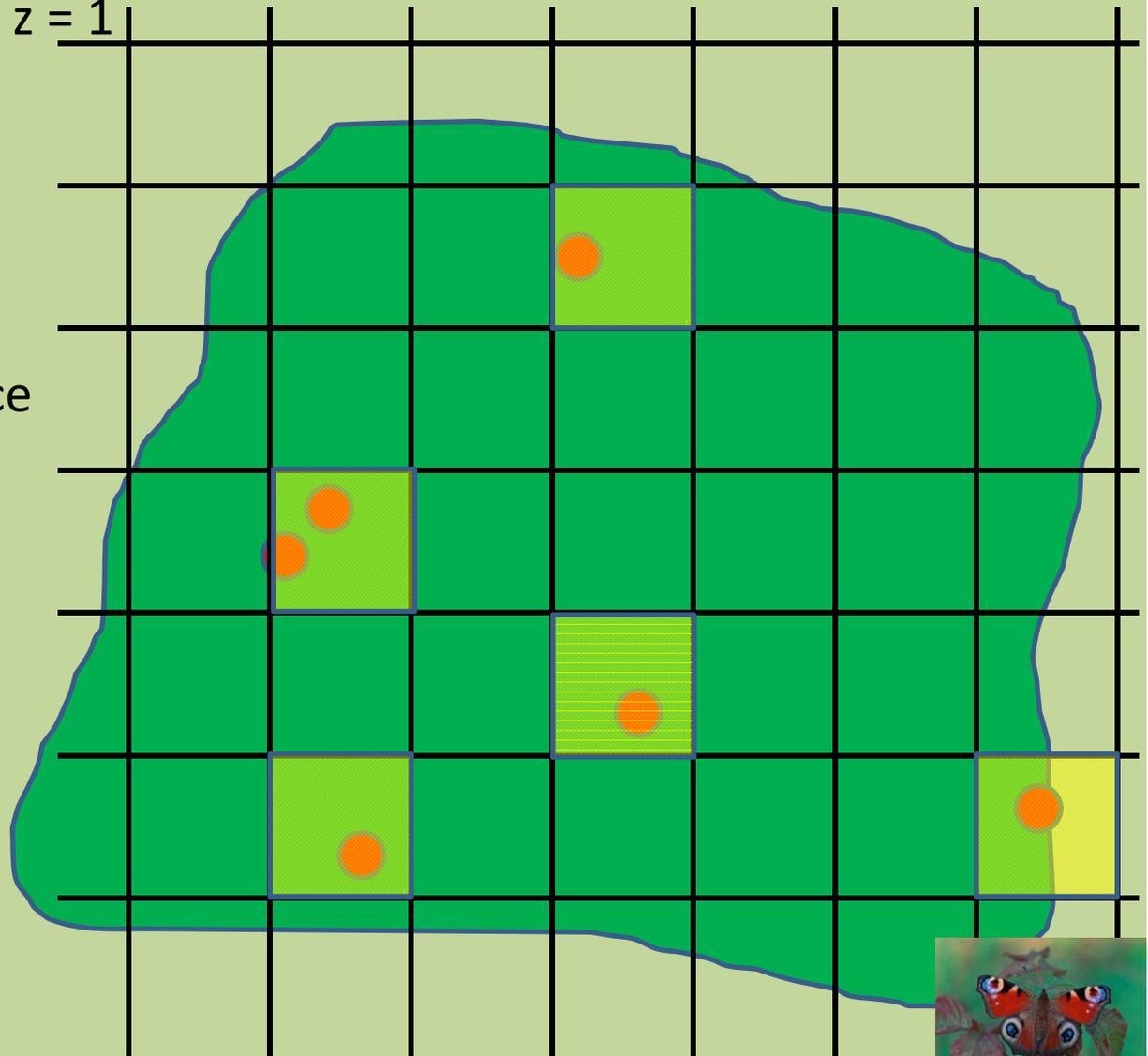
## Mathematical relationship between distribution and abundance

- Occurrence/Presence:  $z = 1$
- Presence  $z = 1$  if  $N > 0$
- Absence  $z = 0$  if  $N = 0$



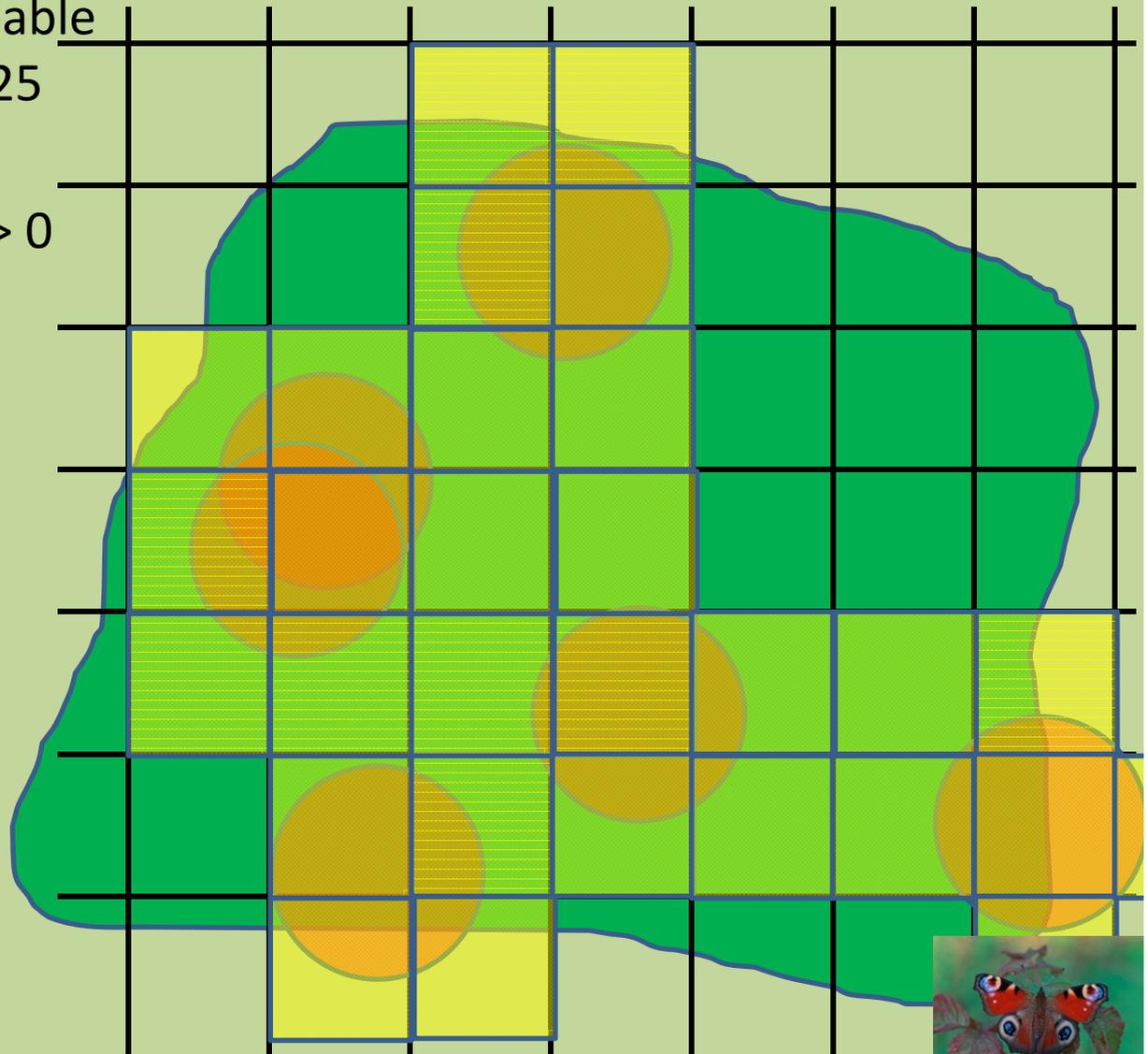
## Mathematical relationship between distribution and abundance

- Occurrence/Presence:  $z = 1$
- Presence  $z = 1$  if  $N > 0$
- Absence  $z = 0$  if  $N = 0$
- Distribution = information-reduced summary of abundance for some areal unit
- **AND:**  
**Both distribution & abundance areal-summary of spatial point process**



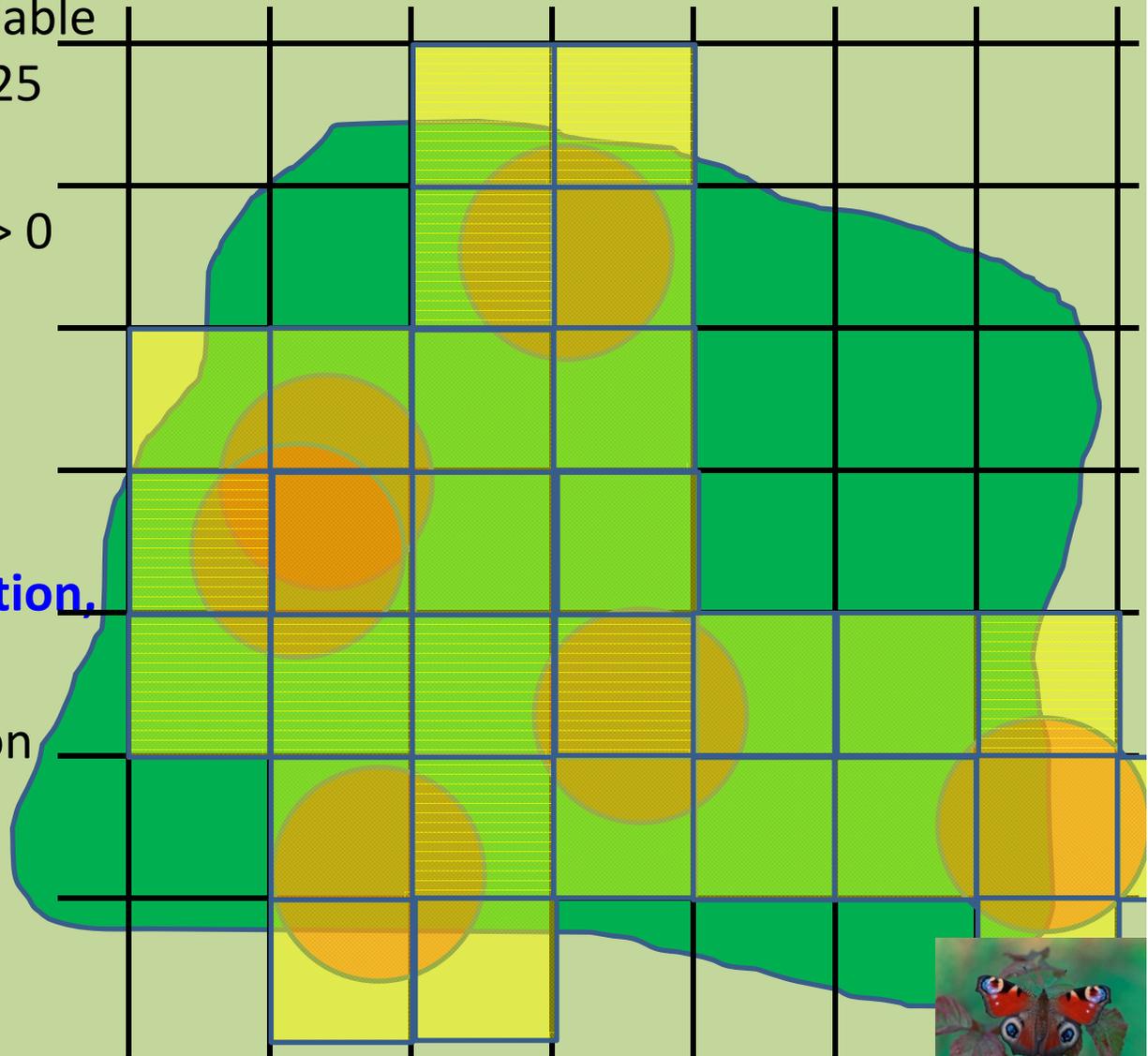
## And what if there is movement (home-range) ?

- **New:**  $N$  is random variable  
 $E(N)$  fractional, e.g. 0.25
- Same:  
Presence  $z = 1$  if  $E(N) > 0$
- Same: Distribution =  
information-reduced  
summary of expected  
abundance



## And what if there is movement (home-range) ?

- **New:**  $N$  is random variable  
 $E(N)$  fractional, e.g. 0.25
- Same:  
Presence  $z = 1$  if  $E(N) > 0$
- Same: Distribution =  
information-reduced  
summary of expected  
abundance
- **New: greater distribution,**  
“use” vs. “presence”
- Same: Both distribution  
& abundance areal-  
summary of SPP



## Section summary: what is occurrence/distribution ?

- Individual animals and plants small & discrete units (not continuous like sea surface temperature)
- Spatial point patterns !
- Fundamentally, abundance and species distribution both areal summary of spatial point patterns (= realisations of spatial point process)
- Occurrence (and distribution) is information-poor summary of abundance:  $z = I(N > 0)$
- Continuous maps imply discrete spatial units, within which point pattern is summarized
- “Distribution” meaningless without:
  - (i) definition of occurrence
  - (ii) definition of spatial unit (pixel size)
  - (iii) spatial scale of organism movement (if any)
  - [ (iv) temporal scale ]



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# The ugly truth about all distribution & abundance data

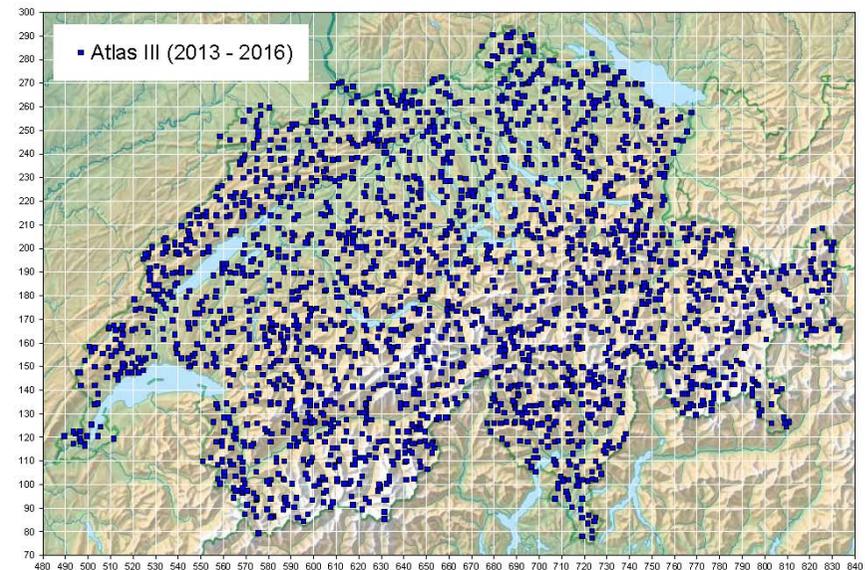
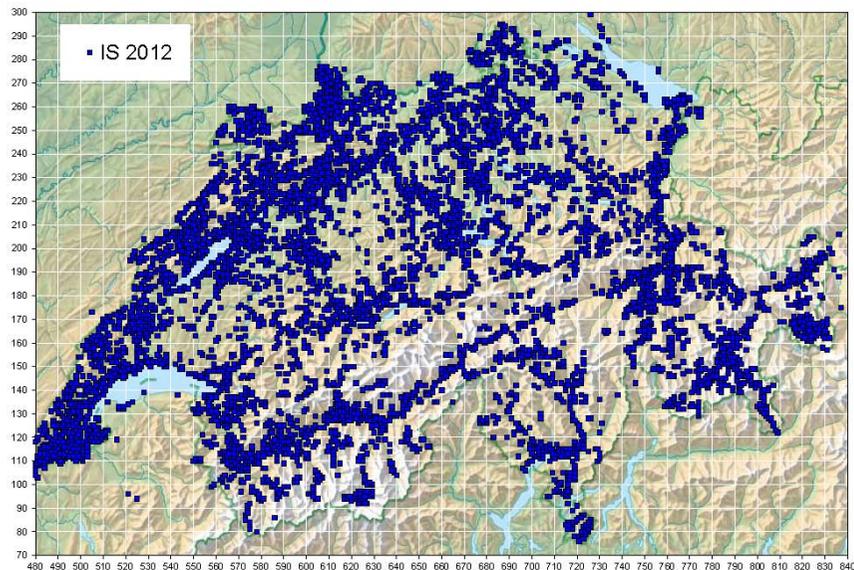
## First complication: Spatial sampling

- Don't observe it in the entire domain about which you want to learn something, or, spatial heterogeneity in effort
- (OK, can predict ...)
- probability to get observation at a site may be related to the measurement (e.g., sites with some values of  $N$  or  $z$  or of covariates  $X$  may be more or less likely to be sample)
  - -> missing not at random (MNAR); non-ignorable missing value mechanism in statistics !
- Has to be modelled to avoid bias
- **Spatial sampling (i.e., *where* measurements are made) can be very important in ecology and management**



## The ugly truth about all distribution & abundance data

- e.g., Swiss citizen-science program IS and designed Atlas III
- In principle, extrapolation based on:
  - random sampling
  - covariate relationships
  - Neighbourhood relationships



# The ugly truth about all distribution & abundance data

## Second complication: Measurement errors

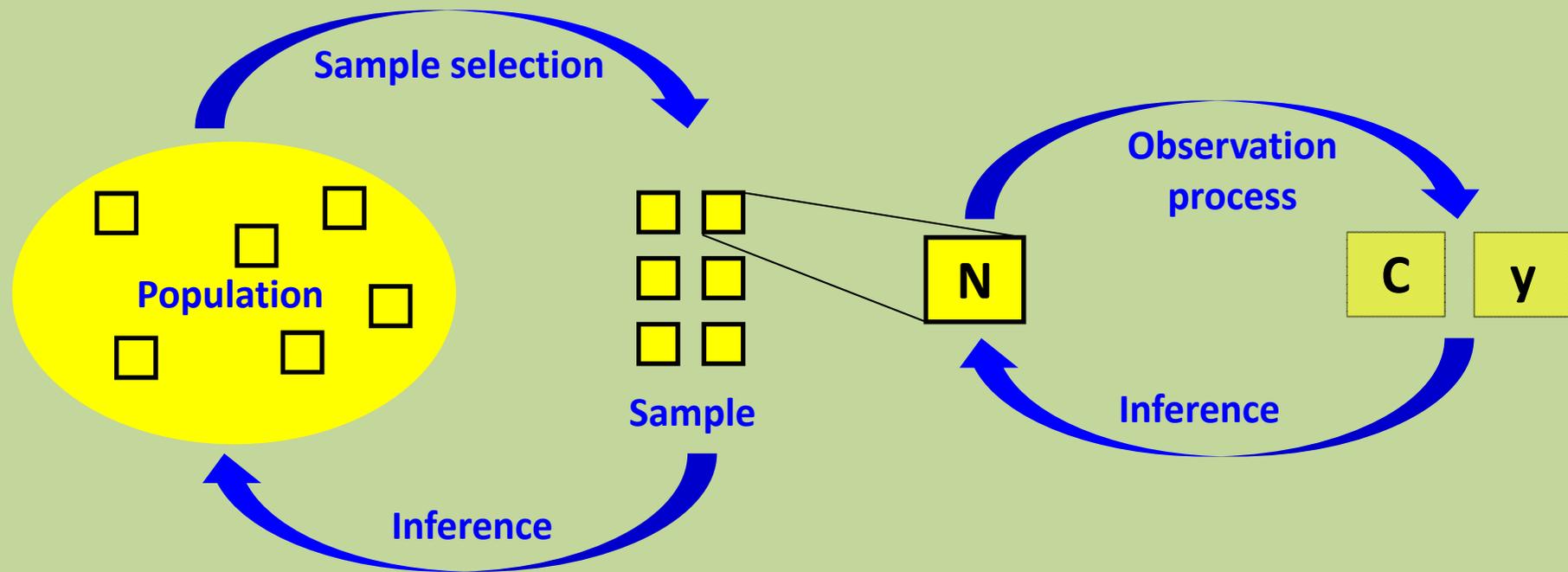
- Two kinds for counts and occurrence data:
  - “Individuals” overlooked when present:
    - > false negative errors
  - “Individuals” misidentified/counted doubly:
    - > false positive errors
- induces non-ignorable missing values (MNAR)
- Biased inference unless missingness process modelled
- Missingness = measurement process = observation process
- **Measurement error processes can be important for all analyses in ecology and management**



# The ugly truth about all distribution & abundance data

Spatial sampling process

Measurement error process



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## Kinds of data on distribution and abundance

- Presence-only data:
  - invent pseudo-zeroes and do logistic regression (bad)
  - use background sample and do MaxEnt or Maxlike (less bad)
  - treat as spatial point pattern and do SPP modeling, e.g., R package spatstat (difficult: assumptions, statistics), also powerful INLA quasi-R-package
- Presence/absence: variant of logistic regression: GLM, GAM, BRT
- Presence/absence data replicated in time: site-occ. modeling
- Count data, with or without replication in time: Poisson GLM or Nmix modeling
- **Note:** presence/absence is misleading term, used for convenience only



## Value of hierarchical modeling for ecological modeling

- Hierarchical models natural framework for ...
- ... *thinking* about processes underlying all ecological field data; ecological and measurement
- ... *describing*, in a model, these processes
- ... that is, for **mechanistic modeling** in ecology
- and, to *analysing* ecological data on distribution and abundance, while accounting for spatial sampling and (non-ignorable) measurement error processes

